Areal-averaged trace gas emission rates from long-range open-path measurements in stable boundary layer conditions

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Abstract. Measurements of land-surface emission rates of greenhouse and other gases at large spatial scales (10,000 m²) are needed to assess the spatial distribution of emissions. This can be readily done using spatial-integrating micrometeorological methods like flux-gradient methods which were evaluated for determining land-surface emission rates of trace gases under stable boundary layers. Non-intrusive path-integrating measurements are utilized. Successful application of a flux-gradient method requires confidence in the gradients of trace gas concentration and wind, and in the applicability of boundary-layer turbulence theory; consequently the procedures to qualify measurements that can be used to determine the flux is critical. While there is relatively high confidence in flux measurements made under unstable atmospheres with mean winds greater than 1 m s⁻¹, there is greater uncertainty in flux measurements made under free convective or stable conditions. The study of N₂O emissions of flat grassland and NH₃ emissions from a cattle lagoon involves quality-assured determinations of fluxes under low wind, stable or night-time atmospheric conditions when the continuous “steady-state” turbulence of the surface boundary layer breaks down and the layer has intermittent turbulence. Results indicate that following the Monin-Obukhov similarity theory (MOST) flux-gradient methods that assume a log-linear profile of the wind speed and concentration gradient incorrectly determine vertical profiles and thus flux in the stable boundary layer. An alternative approach is considered on the basis of turbulent diffusivity, i.e. the measured friction velocity as well as height gradients of horizontal wind speeds and concentrations without MOST correction for stability. It is shown that this is the most accurate of the flux-gradient methods under stable conditions.

1 Introduction

The determination of trace gas and especially greenhouse gas (GHG) emission rates from open land is important to understand our climate and current and future changes in climate (Forster et al., 2007). There is high spatial variability of GHG fluxes from soils of the same type and under identical management (Turner et al., 2008). A better knowledge of the temporal and spatial variations of the trace gas fluxes requires an up-scaling of sources and sinks measurements near the surface (Denman et al., 2007). Up to now, a large amount of trace gas emission measurements has been done by time-dependent accumulation of gasses in small (less than 1 m²) but variously-sized chambers (see e.g. Butterbach-Bahl et al., 2004). A possible larger-scale measurement technique of this sort is the time-dependent accumulation of trace gases in a measuring tunnel with open-path optical methods like FTIR (Fourier Transform InfraRed spectrometry), DOAS (Differential Optical Absorption Spectroscopy) or TDLAS (Tunable Diode Laser Absorption Spectroscopy) along the longitudinal tunnel axis, which yields path-integrated concentration (PIC) values (see e.g. Galle et al., 1994; Schäfer et al., 2012). Measurements of fluxes at larger spatial scales
give results comparable to averaged chamber measurements and "steady-state" conditions cease, the layer can have inter-

turbulence may be representable in path-integrated measure-

determination of gas fluxes from open land during

2 Flux measurement methods

The determination of gas fluxes from open land during stable atmospheric conditions was studied in two different cases. Several flux measurement methods are applied to show and discuss the differences and to propose a methodology to handle stable conditions. Three-dimensional (3-D) sonic anemometers are used to measure wind and turbulence. Two non-intrusive path-integrating measurement methods (FTIR and TDLAS) are utilized for flux calculation.

2.1 Measurement campaigns

Two experiments were conducted: one at Fuhrberg, Germany and one at Indiana, USA. The Fuhrberg experiment was performed in a Festuca rubra field of 20–40 m thick sand. N₂O soil emission studies were performed at this flat grassland, which had last been tilled in July 2005, from 2006 until 2008 (Deurer et al., 2008). The Indiana experiment was conducted around an actively-used cattle lagoon (dairy waste la-

2.1.1 Micro-meteorological N₂O emissions of a flat grassland (Fuhrberg experiment)

Gaseous emissions of N₂O were determined from wind and turbulence measurements made by 3-D sonic anemometers and gas concentration measurements using an open-path FTIR during two campaigns (15–17 October 2007 and 17–19 June 2008). The concentration differences of N₂O, CO₂, CH₄ and H₂O over the field were measured by two bi-static open-path FTIR spectrometers (Griffith, 2002) K300 from Kayser-Threde (Haus et al., 1994): one at 2.70 m a.g.l. (above ground level), z⁺ = 2.70 m, and one at 0.5 m a.g.l., z⁻ = 0.50 m (Fig. 1). Both FTIR paths were 98 m in length and parallel to each other. The lower measurement

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Table 1. Data which have been filtered at all heights for the quality-assured determinations of fluxes under low wind, stable or night-time atmospheric conditions and acceptable ranges for the various parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Phenomenon evaluated</th>
<th>Acceptable range/criterion</th>
<th>Fuhrberg</th>
<th>Indiana</th>
</tr>
</thead>
<tbody>
<tr>
<td>30-min mean wind</td>
<td>directional shear between the heights</td>
<td></td>
<td>$&lt;10^\circ$</td>
<td>$&lt;20^\circ$</td>
</tr>
<tr>
<td></td>
<td>wind direction variation</td>
<td>within 45° of the perpendicular to a measurement plane</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>wind speed limit</td>
<td>&gt;0.1 m s$^{-1}$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>perturbation of wind components $u'$, $v'$, $w'$</td>
<td>spikes</td>
<td></td>
<td>&gt;5 standard deviations above the mean over 5 min,</td>
<td>&gt;80 % of measurements had to be valid</td>
</tr>
<tr>
<td>perturbation of vertical wind component $w'$</td>
<td>intermittency and waves</td>
<td></td>
<td>visual inspection of 30-min means</td>
<td></td>
</tr>
<tr>
<td>vertical turbulence (mean $u'^2$)$\sigma_{w^2}$</td>
<td>analysis of spectral distribution</td>
<td></td>
<td>similarity at both heights</td>
<td></td>
</tr>
<tr>
<td>calculated $\zeta$</td>
<td>analysis of spectral distribution</td>
<td></td>
<td>continuity, consistency across heights</td>
<td></td>
</tr>
<tr>
<td>bulk Richardson number $R_i$</td>
<td>dominance of turbulent production</td>
<td></td>
<td>–</td>
<td>&lt;0.2</td>
</tr>
<tr>
<td>concentration differences across height</td>
<td>consistency</td>
<td></td>
<td>difference &gt; 0 to statistical errors (combined errors with 0.90 levels, t-statistics: factor 1.44)</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>consistency across heights</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 1. Configuration of the Fuhrberg experiments with FTIR spectrometers and radiation sources (globars) showing the measurement paths and sonic anemometers. Chamber measurements were made in about 10 m distance to the one end of the FTIR paths. The measurement volume was oriented in north-south direction.

height was determined to be about 10 times the roughness length of the grassland.

The spectral resolution of the FTIR measurements was 0.2 cm$^{-1}$, allowing the determination of interferences in the spectra and thus a high accuracy of the concentration measurements (Sussmann and Schäfer, 1997). The telescope of the spectrometers for the detection of the IR radiation of the radiation source had a diameter of 15 cm and a field of view of 3 mrad. The measurement time was about 5 min. The measurements were running continuously, interrupted by short time periods for internal alignment procedures of the spectrometers (20 up to 60 min) every 3 up to 6 h. The minimum detection limit (MDL) of the K300 spectrometers at a 100 m open path was 5 ppb (10 µg m$^{-3}$) for N$_2$O. The statistical concentration measurement error was less than 3 % (Haus et al., 1994) and was calculated from the signal-to-noise-distance in the measured spectra for each measurement. This detection limit and measurement precision were appropriate to detect concentration differences of more than 1 %. Griffith et al. (2002) and Esler et al. (2000), who used FTIR for micro-meteorological techniques as closed-path measurement method, found similar values. The temporal variations of the measured greenhouse gas concentrations at both heights followed the expected daily courses. The data quality filtering criteria are given in Table 1.

The 3-D sonic anemometers (USA-1) from Metek GmbH measured the wind and turbulence at the same heights as the FTIR open paths. Corresponding to the upper height the fetch or footprint, i.e. the required homogeneity in upwind direction, was about 270 m. Considering the path lengths of about 100 m, the investigated area was about 27 000 m$^2$.

A comparison of both open-path FTIR instruments was performed (22 and 23 November 2007 as well as 10 and 11 July 2008) following each flux-gradient measurement campaign. A 1 h inter-comparison of the mean winds measured by the two 3-D sonic anemometers was also performed, but this was completed in the field during the campaigns. The comparison-measured bias between FTIR spectrometers was
used to correct the measured differences for each measurement campaign. No bias corrections were needed for the 3-D sonic anemometers.

### 2.1.2 Chamber \( \text{N}_2\text{O} \) emission of a flat grassland (Fuhrberg experiment)

Gaseous emissions were determined from the time rate of change of \( \text{N}_2\text{O} \) concentration in four closed chambers per time period measured. The chambers (area of 0.045 m\(^2\) each) were located on a plot of 1.5 m by 1.5 m in the vicinity of the micro-meteorological emission measurements (Sect. 2.1.1). Gas samples were collected in ambient air before closing of the chambers and every 20 min over 1 h after the closing. Measurements were performed the day following the open-path flux-gradient measurements at around 22:00 LT. Concentrations of \( \text{N}_2\text{O} \) were analysed from the gas samples using a gas chromatograph (Fisons GC 8000, Milan, Italy) equipped with a split-injector, an electronic capture detector and a HP-Plot Q column (30 m length \( \times \) 0.32 mm ID; Agilent Technologies, Santa Clara, USA). The gas samples were analysed within 3 weeks after the collection (Weymann et al., 2009; von der Heide et al., 2009).

The \( \text{N}_2\text{O} \) fluxes were determined and qualified for use by the linearity of the increases/decreases of the concentration measurement. As the \( \text{N}_2\text{O} \) fluxes were very low, we chose a linearity criterion of the square of regression coefficient of 0.8. If this coefficient was smaller than 0.8, the flux rate of the chamber was set to zero. The non-steady-state diffusive flux estimator (NDFE) method of Livingston et al. (2006) was also used to determine the flux.

### 2.1.3 Micro-meteorological \( \text{NH}_3 \) emissions from a cattle lagoon (Indiana experiment)

Gaseous emissions of \( \text{NH}_3 \) were determined from wind measurements made by 3-D sonic anemometers (R. M. Young sonic 8100) and open-path gas concentration measurements using TDLAS (GasFinder 2.0, Boreal Laser, Inc). Measurements were made for a total of 321 days between September 2008 and August 2009.

Concentration gradients of \( \text{NH}_3 \) were determined from scanning TDLAS measurements. The TDLAS units were set up at opposite corners of the 85 m by 116 m lagoon with 16 m towers placed at the other two corners of the lagoon (Fig. 2). Open-path \( \text{NH}_3 \) measurements were made along each adjacent side of the lagoon at 0.9 m a.g.l. along paths extending about 1/3 rd and 2/3 rds and slightly more than the full distance down the side of the source and at two vertical angles to retro-reflectors between 85 m and 116 m away and at approximately 7.6 m a.g.l. and 15.2 m a.g.l. Thus, each side of the source has three near-surface paths and two elevated paths. The scanner sequentially aimed the TDLAS at one of the ten retro-reflectors on the two adjacent sides of the source such that a complete set of measurements occurred every 100 s.

Fig. 2. Configuration of Indiana experiment. The scanning TDLAS (open circle), retro-reflectors (filled squares), towers (yellow squares) and open paths (solid lines) are shown with the height of the equipment indicated in meters.

Quality control (QC) checks for the TDLAS measurements included checks for path obstruction at every measurement, internal calibration checks at every 100 measurements, spectral feature check and single point calibration verification approximately every 21 days, and multi-point calibrations every six months. Based on twice the precision, the TDLAS units had a minimum detection limit of 2 ppm m or less. The TDLAS calibration was verified at 50 ppm m using a 0.5 m calibration cell in an approximately 4 m path length. Spectral feature checks were made using a digital oscilloscope.

The 3-D sonic anemometers were mounted at 2.5 m (\( z^- \)), 4.4 m (\( z^F \)), and 16.2 m (\( z^+ \)) height (Fig. 2). The wind speed and temperature gradient measurements were assured by frequent inter-comparisons of the three sensors in the field and three “reference” (unused except for calibration checks) anemometers. The comparison-measured bias between the temperature measurements of the sonic anemometers was used to correct the measured temperature gradients. No bias corrections were needed for the sonic anemometer wind measurements.

The TDLAS \( \text{NH}_3 \) MDL was determined to be approximately 30 ppb (13.9 µg m\(^{-3}\)) for the paths measured in the campaign. The statistical concentration measurement error across the measurement domain was measured at less than 5 % based on calibration verifications.

Since the flow often has the lagoon upwind and the lagoon berm is both a roughness and height transition, we might expect convergence with turbulence regularly advected across the measurement planes.

The multiple downwind measurements in the plume in vertical planes perpendicular to the wind direction are also used for the integrated horizontal flux (IHF) method. These results are applied for comparison with the flux-gradient method.
2.2 Sonic anemometers and quality assurance checks

While 3-D sonic anemometer measurements were aligned to the natural wind coordinates for the Fuhrberg experiment conducted over a flat open field, they were not aligned in the Indiana experiment because the measurements were made in close proximity to a lagoon with a 1–3 m drop in elevation to the lagoon liquid surface. Turbulence statistics (variances and co-variances) were calculated for all heights except 0.5 m where it was expected that significant fractions of the turbulence would not be measurable by the sonic anemometer. The momentum flux and sensible heat flux were determined by the eddy-covariance method (Foken, 2008). The Monin-Obukov length $L$ was determined with $\theta^*$ (perturbation in the virtual potential temperature), approximated by $\theta^*_s$ (perturbation in sonic anemometer temperature), and $w^*$ (perturbation of the vertical wind speed). Since there is often a strong self-correlation between the turbulence quantities used in the calculation of $L$ and the gradient Richardson number is vulnerable to significant errors when the vertical wind profile is complex, the bulk Richardson number $Ri_B$ was used as an additional measure of overall stability (Mahrt, 2010).

The nature of the flow variability during each measurement period was evaluated. Tests used to evaluate the nature of the flow variability are summarized in Table 1 together with the acceptable ranges for the various parameters. The inter-comparisons during the Indiana experiment showed a mean difference between the field-used 3-D sonic anemometers and the reference anemometers of 0.03 m s$^{-1}$ and up to 3 K. Temperature bias between sonic anemometers was corrected prior to determination of $Ri_B$. During the Fuhrberg experiment typically differences between sensors were less than 0.1 m s$^{-1}$, zero flow check resulted in a flow of less than ±0.05 m s$^{-1}$.

Influences of non-turbulent motions and non-homogeneous, unsteady flow were partially excluded from the data set by restrictions on the acceptable values of $Ri_B$ (Fig. 3). Distinct non-turbulent waves were evident in many of the most stable periods in the Indiana experiment: a $Ri_B$ of less than 0.2 corresponded to boundary layers with distinct (although sometimes weak) turbulence, consistent with theory (Luhar et al., 2009). The removal of all measurement periods where $Ri_B > 0.2$ (Fig. 3) reduced the range of the stability $\zeta = (z-d)/L$, where $d$ is the displacement height (0.134 m for the Fuhrberg experiment and assumed zero for the Indiana experiment), to values less than 0.8 (Fig. 4) and the quality-assured dataset to 358 30-min measurement periods. Even with this exclusion, the deviation of the stability correction function $\psi_c$ from the theoretical relationship with $\zeta$ (Fig. 4) implies non-stationarity of the flow associated with waves, meandering flow and other coherent flow structures (Mahrt, 2007). Consequently, we also then expected differences between the diffusivity-based flux calculation and the MOST-theory based flux-gradient calculations since non-stationarity often results in more linear (not logarithmic) wind profiles (Mahrt, 2007).

2.3 Micro-meteorological emissions methods

Emissions were calculated (1) using the IHF method as well as (2) by a flux-gradient method using (2a) turbulent diffusivity as exchange coefficient (termed “similarity” method), (2b) using a MOST-parameterized stability correction to the

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**Figure 3.** Relationship between the two measures of overall stability – stability $\zeta$ from bulk Richardson number $Ri_B$ – during the Indiana experiment. The critical $Ri_B$ (dashed line) and BDH relationship (empirically-derived values from Businger et al., 1971, Dyer, 1974 and Hicks, 1976) below critical $Ri_B$ (solid line) are indicated.

**Figure 4.** Relationship for the trace gas stability correction function $\psi_c$ between the dependence of integrated profile at 4.4 m ($z_F$) based on measurements at 2.5 m ($z^-\) and 16.2 m ($z^+$) on stability $\zeta$. The measured values (circles) and the nominal relationships according to Holtslag and de Bruin (1988) (solid line) are indicated. The remaining data after the quality assurance procedure stated in the text are red.
MOST theorized wind and concentration profile (termed “parameterized” flux-gradient method), and (2c) that replaces the parameterizations for $c_a$ and $u_a$ with measurements (termed “measured $u_a^*$” flux-gradient method).

### 2.3.1 Open-path integrated horizontal flux method (IHF)

Emissions of NH$_3$ during the Indiana experiment were determined at 30-min intervals from wind profiles based on the three anemometers and concentration profiles based on the multiple TDLAS-measured PIC using the vertical radial plume mapping method (Hashmonay et al., 2001). This method utilizes the product of an interpolated mass concentration distribution and interpolated wind speed normal to the measurement plane and is therefore fundamentally an IHF method. Only measurement periods with valid measurements for all five PICs of a measurement plane for the entire 30-min period were included in the analysis. Comparisons between the IHF and the various flux-gradient methods discussed above were limited to periods of measurement when only one of the four planes had a measured flux. Because of the mismatch in sampling intervals between the sonic anemometer and the TDLAS, some of the flux measured by the IHF method would be a result of the covariance between horizontal wind perturbations and gas concentration perturbations (Denmead, 2008). We expect an overestimation of the flux using the IHF method of 5 to 20\%. Background concentrations of NH$_3$ and the corresponding flux were assumed negligible.

### 2.3.2 Open-path flux-gradient measurement methods

Steady-state turbulence in the surface boundary layer and height-constant conditions were assumed for all flux-gradient methods. The “parameterized” flux-gradient method multiplies a parameterized friction velocity $u_a$ by the corresponding concentration scaling parameter $c_a$ according to MOST to get the flux (Foken, 2008). $u_a$ [m s$^{-1}$] was estimated according to Lege (1981) and the stability correction for trace gases was assumed to be identical to that for momentum (see e.g. Holtslag and de Bruin, 1988). The empirically-derived values are from Businger et al. (1971), Dyer (1974) and Hicks (1976) (termed BDH). The stability correction was estimated according to the suggested equations of Holtslag and de Bruin (1988). During the campaigns, $\psi_c$ showed the expected relationship to $\zeta$ with the exception that the values crossed the $\zeta = 0$ line below the expected value of $\psi_c = 0$ (Fig. 4). This suggests that either turbulence was advected into the profiles, variance in the motion of the boundary layer was associated with non-turbulent structures, and/or the wind profile was not log-normal. Although non-turbulent variance in motion associated with waves at high $\zeta$ also contribute to deviations from the theoretical relationship, periods with such motion were largely excluded from the analysis using procedures described below.

The “measured $u_a^*$” flux-gradient method replaces the parameterizations for $c_a$ and $u_a$ with measurements: if the wind and concentration measurements are at the same heights, $\psi_c$ can also be based on the measured values of $u_a$ by solving the $u_a$ equation for $\psi_c$; and if the wind and concentration measurements are at different heights, $\psi_c$ can be parameterized, while $u_a$ is determined directly from the sonic anemometer measurements.

The “similarity” method uses fewer assumptions than the “parameterized” or “measured $u_a$” flux-gradient methods in that there is no assumed MOST correction for stability and no assumed neutral MOST logarithmic wind profile. The turbulent diffusivity $K_c$ was calculated from the measured friction velocity $u_a$ (mean of the measured friction velocities in the heights $z^+$ and $z^-$, see also Stull, 1997) and the measured height difference of the horizontal wind speeds $u$ [m s$^{-1}$] by

$$K_c = \frac{1}{Sc} \frac{u_a (z_F)^2}{u(z^+) - u(z^-)} \frac{z^+ - z^-}{z^+ - z^-},$$

where $Sc$ is the Schmidt number and $z_F$ [m] is the height of flux calculation. Lacking knowledge of the turbulent $Sc$, we assume that the molecular value is a good first approximation of the turbulent $Sc$. The molecular $Sc$ is 1.079 for N$_2$O and 0.63 for NH$_3$ (Massman, 1998). The flux $F$ is then calculated with the vertical gradient of the concentration $c$ [µg m$^{-3}$] as:

$$F (z_F) = -K_c \frac{dc}{dz} = -K_c \frac{c(z^+) - c(z^-)}{z^+ - z^-}.$$

### 2.4 Application of open-path measurements for flux calculations

The vertical N$_2$O gradients were based on the quality-assured open-path FTIR measurements made ground-parallel. Concentration and wind measurements were made at 2.70 m and 0.5 m a.g.l.

The vertical NH$_3$ gradients were derived from the slant-path measurements by defining three layers (0–2.6 m, 2.6–8 m, and 8–15.2 m) and assuming the gas is uniformly mixed within each layer. The concentrations of each layer were then determined by sequentially solving three equations with three unknowns; where the fractional length of the overall measurement path through each layer is known, the concentration through the entire layer is assumed uniform and the cumulative concentration of gas along the entire path is measured (see also Table 1). The wind gradient at 4.4 m height was determined from the wind measurements made at heights of 2.5 m and 16.2 m, $\xi$ determined from the 4.4 m sonic anemometer height, and the concentration gradient at 4.4 m height was determined from the gradient approximated from horizontal gradients of NH$_3$ based on the TDLAS measurements.
The MDL of each flux-gradient methodology was evaluated assuming that the measurement errors are independent (Taylor, 1982). An analysis of the propagation of measurement errors for the “parameterized” flux-gradient method indicated a MDL of approximately 5 % for the FTIR-based open-path measurement method and 12 % for the both TDLAS-based open-path measurement method. The \( K_c \) MDL was approximately 0.01 \( \text{m}^2\text{s}^{-1} \) for the FTIR-based measurement method and 0.002 \( \text{m}^2\text{s}^{-1} \) for the TDLAS-based measurement method. It is important to understand that these errors are only the propagation of measurement errors through the equations and not associated with the ability of a given method to describe the true flux given the variability in the environment.

3 Results

Results are shown for the turbulence measurements and the flux determination by the different methods during both campaigns.

3.1 Atmospheric dynamics aspects

The atmospheric conditions during the Fuhrberg experiment were similar to the stable boundary layer measurement periods of the Indiana experiment. In both experiments, the concentration gradient range in \( \text{NH}_3 \) (0.6 to 114.6 \( \mu \text{g m}^{-3} \text{m}^{-1} \)) and \( \text{N}_2\text{O} \) (4.4 to 22.0 \( \mu \text{g m}^{-3} \text{m}^{-1} \)) increased with decreasing wind speed (Fig. 5). There was no distinct relationship between the vertical \( \text{NH}_3 \) and \( \text{N}_2\text{O} \) concentration gradients and the vertical gradient in horizontal wind speed, however there was a tendency for greater concentration gradients corresponding to low horizontal wind speed gradients less than 0.2 \( \text{m s}^{-1} \). The maximum observed \( \zeta \) however differed somewhat: 0.81 in the Indiana experiment and 1.16 in the Fuhrberg experiment.

The turbulent conditions during the quality-assured 30-min periods were also similar in both experiments (Fig. 6a), with the calculated \( K_c \) for both experiments decreasing with decreasing wind gradient and \( u_z \) and decreasing with increasing \( \zeta \) for all stable measurement periods (normalized by \( Sc \) in Fig. 6b and d). The wide range in possible \( K_c \) for a given wind speed gradient was a result of small gradients developing either under high winds under near-neutral stability or low winds. Note that the \( ScK_c \) does not approach the molecular diffusivity of the order \( 10^{-5} \text{m}^2\text{s}^{-1} \) as \( \zeta \) increases to 1.0 (Fig. 6c). This was probably largely a result of the MDL for the measured \( K_c \), although it may also indicate the predominance of turbulent mixing over molecular mixing for the weak, often intermittent turbulence of the stable boundary layer. Note that the quality assurance minimized the influence of waves and other coherence structures on the calculated \( ScK_c \).

3.2 \( \text{NH}_3 \) emission fluxes from a lagoon

It was assumed that the flux determined from the IHF method was closest to the actual flux. The \( \text{NH}_3 \) flux calculated by IHF varied from near zero to 330 mg m\(^{-2}\) h\(^{-1}\) (mean 90 mg m\(^{-2}\) h\(^{-1}\)), with 49 30-min measurements with \( \zeta \) between 0 and 0.01, 139 with \( \zeta \) between 0.01 and 0.1, 86 with \( \zeta \) between 0.1 and 1.0. A negative flux indicated flux to the lagoon from the surroundings. The IHF estimates of \( \text{NH}_3 \) flux in the Indiana experiment are homogeneously spread around a relationship from logarithmic \( \zeta \).

There is an IHF positive bias due in part to the inability of the method to quantify a “plume” when the concentration field is near background values and in part to the inclusion of turbulent diffusive fluxes (Denmead, 2008). \( \text{NH}_3 \) flux calculated using the three flux-gradient methods were generally lower than the IHF method (Fig. 7). This tendency was probably in part due to errors in the calculated vertical \( \text{NH}_3 \) concentration gradients described previously. Since this error was present for all three flux-gradient methods, a comparison of the three methods can still give useful information concerning the ability of each method to approximate the IHF. The correlation \( r \) between the “parameterized” flux-gradient and the IHF method was 0.53, with root mean square error (RMSE) of 43 mg m\(^{-2}\) h\(^{-1}\) (solid line, Fig. 7). The regression for the “parameterized” flux comparison is driven by three outlying values that are not indicated in Fig. 7: the dashed line indicates the linear regressions without outliers less than zero and greater than 180 mg m\(^{-2}\) h\(^{-1}\). Removing these outliers dramatically improves the correlation between the IHF and the “parameterized” methods to \( r = 0.61 \) with negligible change in the RMSE (40 mg m\(^{-2}\) h\(^{-1}\)).

Calculating the flux based on the measured wind profile resulted in a better relationship to the IHF method than the “parameterized” method: \( r = 0.68 \), RMSE = 38 mg m\(^{-2}\) h\(^{-1}\) (Fig. 7). The use of the measured \( u_z \) in place of the parameterized \( u_z \) prevented the outlying flux estimates and
Fig. 6. Variation in vertical turbulence $\sigma_w$ and the product of Schmidt number with turbulent diffusivity $ScK_c$ at the flux calculation height with horizontal wind speed gradient below that height – panels (A) and (B), and variation in $ScK_c$ with stability $\zeta$ (C) and friction velocity $u_*$ (D) at that height. Values in both the Indiana (open circles) and Fuhrberg (closed red circles) experiments are indicated.

Fig. 7. The comparison between the IHF method and the flux-gradient method using $K_c$ of “similarity” approach according to Eqs. (1) and (2), of “parameterized” approach with theoretical friction velocity $u_*$ and stability correction function $\psi_c$ as well as of “measured $u_*$” approach. Linear regressions between the flux measures are indicated by solid lines. The dashed line at “parameterized” flux comparison indicates the linear regressions when outliers less than zero and greater than 200 mg m$^{-2}$ h$^{-1}$ are neglected.

Consequently is an improvement on the parameterization of $u_*$ (Fig. 7), with the greatest flux related to less stable conditions (Fig. 8).

The difference between the flux calculations using the parameterization of $u_*$ and the measurement-based $u_*$ suggested the wind profile was not log-linear as implied in the analysis of $\psi_c$ (Fig. 4), reducing the utility of the parameterization to describe the gradient. This is consistent with the finding that the wind profile is commonly more linear than log-linear in the stable boundary layer (Mahrt, 2007). These non-log-linear wind profiles within the measured layer strongly influenced the flux.

The NH$_3$ flux calculated using the “similarity” method assumed linear profiles rather than a log-linear profile of wind and concentration. This method resulted in fluxes closer to those determined by the IHF method than the other two methods that assumed log-linear profiles (Fig. 7). The correlation
between the diffusivity method and the IHF method was $r = 0.80$ with a RMSE of 31 mg m$^{-2}$ h$^{-1}$ (Fig. 7).

All flux-gradient methods resulted in estimated fluxes, with the range of values decreasing with increasing $\zeta$ (Fig. 8). This was consistent with mixing theory where mechanical turbulent mixing is suppressed by negative buoyancy to an increasing extent as the stability increases.

### 3.3 N$_2$O emission fluxes from soil

The calculated $K_c$ values for the Fuhrberg experiment were within the range of those calculated from the Indiana experiment and showed similar relationships to the vertical gradient in $u$, $u_*$, and $\zeta$ (Fig. 6). The calculated diffusivity for the Fuhrberg experiment showed a decrease with the increasing stability limited by the measurement errors to values of 0.01 m$^2$ s$^{-1}$ (Fig. 6).

During the first campaign (16–17 October 2007), wind speeds varied from 2.3 m s$^{-1}$ to 0.6 m s$^{-1}$ and the surface boundary layer was characterised by stable and very stable conditions with $\zeta$ up to 8. This extreme stability resulted in minimal valid emissions determinations. Between 14:30 and 20:00 h of 16 October, all wind speeds (above and below) were relatively small with corresponding small wind speed gradients. During this time the difference between the concentration measurements was statistically significant (Fig. 9). Between 22:30 and 24:00 h the measured vertical concentration differences were statistically significant also, resulting in valid flux determinations. After this time, the difference in the two concentrations was again not statistically significant.

There are some gaps in the N$_2$O measurement time series due to the necessity for internal optical adjustment of the spectrometers (Figs. 9 and 10).

During the second campaign, the surface boundary layer had very stable conditions and very low horizontal wind speeds with $\zeta$ up to 11. The N$_2$O concentrations in ambient air (17–18 June 2008) at both heights were not significantly different (Fig. 10).

Chamber measurements of the N$_2$O flux were made on 17 October 2007 after the first campaign when the wind speed at 2.7 m a.g.l. was 0.5 m s$^{-1}$, the air temperature was $10^\circ$C and there was no precipitation. These conditions were similar to those during the flux-gradient measurements. Of the four chambers used, one had an unusually high concentration value after 40 min (value excluded), one failed the linearity criterion and had one unusually high concentration (flux set to 0), one indicated an up-take of N$_2$O (linear regression $-9.2 \mu g m^{-2} h^{-1}$ and NDFE $-13.7 \mu g m^{-2} h^{-1}$), and one indicated flux of 155.5 $\mu g m^{-2} h^{-1}$ by both data analysis methods. The mean of the four chamber measurements was $37 \mu g m^{-2} h^{-1}$ by the linear regression and $36 \mu g m^{-2} h^{-1}$ by the NDFE method.

The quality assurance condition of a significant difference in the concentrations for the flux-gradient method was fulfilled in only 22 30-min mean measurements of the two campaigns. Exclusions of measurement periods with high wind shear or strong waves during the averaging period resulted in valid flux-gradient measurements for only 8 of 56 30-min
measurement periods. The calculated emission fluxes decrease with increasing $z$ (Fig. 11).

The $N_2O$ flux was measured by the chamber method on 19 June 2008 after the second campaign. The meteorological conditions were similar as on 17 and 18 June: no precipitation, a wind speed at 2.7 m a.g.l. of 0.7 m s$^{-1}$, and an air temperature of 13°C. Of the four chambers measured; one set of concentration measurements failed the linearity criteria and was assumed to be zero but was calculated as 18.4 $\mu$g m$^{-2}$ h$^{-1}$ by the NDFE method. The other chambers indicated: (1) a flux of 267.7 $\mu$g m$^{-2}$ h$^{-1}$ by both methods, (2) a flux of 97.8 $\mu$g m$^{-2}$ h$^{-1}$ by linear regression and 113.6 $\mu$g m$^{-2}$ h$^{-1}$ by NDFE method, and (3) a flux of 146.2 $\mu$g m$^{-2}$ h$^{-1}$ by linear regression and 1029.6 $\mu$g m$^{-2}$ h$^{-1}$ by NDFE. The mean measured flux was 128 $\mu$g m$^{-2}$ h$^{-1}$ using the linear regression method and 357 $\mu$g m$^{-2}$ h$^{-1}$ for the NDFE method.

The difference between the mean of the $N_2O$ emission rate results using the open-path flux-gradient methods during stable conditions averaged 236 $\mu$g m$^{-2}$ h$^{-1}$ using the “parameterized” approach, 498 $\mu$g m$^{-2}$ h$^{-1}$ using the “measured $u_*$” approach and 903 $\mu$g m$^{-2}$ h$^{-1}$ using the “similarity” approach. Although similar, the average emission from the chamber measurements using the NDFE simulation was 313 $\mu$g m$^{-2}$ h$^{-1}$ (Fig. 11), which were performed at a time difference of one day in October 2007 and two days in June 2008.

The calculated $N_2O$ emission rates from the chambers and the flux-gradient methods agree with the order of magnitude of chamber and box flux measurements from other grasslands. Dittert et al. (2005) found $N_2O$ fluxes of 2 to 19 $\mu$g m$^{-2}$ h$^{-1}$ over similar soils in Northern Germany grassland. Goossens et al. (2001) determined $N_2O$ fluxes from 10 to 2200 $\mu$g m$^{-2}$ h$^{-1}$ from Belgian grassland.

4 Data interpretation and discussion

Assuming the IHF method provided the most accurate flux estimate, the fluxes calculated in the Indiana experiment using the “similarity” method that correlated better with the IHF method than the MOST flux-gradient methods were the most accurate of the flux-gradient methods considered. Since the MOST flux-gradient methods were based on the “measured $u_*$” or “parameterized” approach, it appears that the MOST flux-gradient methods incorrectly assumed log-linear profile of the wind speed and concentration gradient in the stable boundary layer. Consequently it was assumed that the “similarity” method provided the best estimate of $N_2O$ flux in the Fuhrberg experiment also.

The similarity-based $N_2O$ fluxes at Fuhrberg exhibited similar variability with respect to stability as the Indiana experiment, and were comparable to the mean $N_2O$ flux measurements made at Fuhrberg by other methods as well as reported in the literature.

The “similarity” method resulted in the highest fluxes of all the flux-gradient methods considered for both the Indiana and Fuhrberg experiments (Figs. 8 and 11). The flux based on a measured $u_*$ was similar but generally greater than that based on the MOST parameterization in both the Indiana and Fuhrberg experiments. All three approaches to calculate the flux using flux-gradient methods showed similar tendencies.
As with the upper emissions bound of the Indiana experiment (Fig. 8), the emission rates during near-neutral conditions were much higher than during stable conditions (Fig. 11). This was likely caused by changes in weather conditions such as higher wind speeds with correlated greater mixing, causing enhanced emission processes of the soil or by higher soil and lagoon temperatures which will change equilibrium gas concentrations. However it is important to remember that near-neutral conditions do not necessarily result in higher emissions, as evidenced by the results for the NH₃ emissions in Indiana (Fig. 8). The negative exponential tendency affects only the maximum possible flux, as a smaller concentration gradient would reduce the flux under near neutral conditions. The range of possible flux values across the range of stability $\zeta$ was evident in the NH₃ fluxes in Indiana (Fig. 8).

The prerequisites for the application of a flux-gradient measurement method include: (1) negligible advection; (2) negligible chemical changes during the transport of air from the footprint to the measurement system; and (3) vertical turbulent exchange in a not too stable, neutral or slightly unstable lower atmosphere ($\zeta \leq 10$). The Fuhrberg field had good visually-determined horizontal homogeneity and the measurement periods reported here showed vertically-consistent turbulence regardless of wind direction (see Foken, 2008, p. 26, and Schmid, 1994). The horizontal homogeneity at the Indiana location was only generally fulfilled due to the close proximity of the lagoon source to the measurement planes. This resulted in variable surface roughness and stability associated with wind direction due to the lagoon apparently influencing the universal wind profile (and the stability influence on the profile) and possibly decreasing the correlations between the IHF and flux-gradient calculation methods. The condition of turbulent linkage between the surface and the height of measurements was verified for the stable conditions studied by restricting analysis to periods with low vertical wind shear, velocity gradient (Indiana experiment only), stability, and consistency of turbulent structure even if those periods are intermittently occurring within the turbulence time history.

5 Conclusions

The use of open-path flux-gradient methods in non-intrusive up-scaling of trace gas fluxes near the surface was demonstrated here for N₂O and NH₃ in stable boundary layers and path lengths of 100 m. A “similarity” approach that does not assume log-linear relationship of wind speed and concentration with height is the best method to approximate the flux under stable conditions ($0 < \zeta < 1$). The determination of flux under these stable conditions however requires careful evaluation of the continuity of turbulence between the surface and the height of measurement for this approach also.

5.1 Advantages and disadvantages of the open-path flux-gradient methods

In general the application of flux-gradient methods for trace gas flux determinations is difficult to use when either there are: (1) low wind speeds with poorly defined wind speed gradients and typically high vertical concentration gradients or (2) high wind speeds with small concentration gradients. Under stable conditions the weak and intermittent turbulence further restricts the use of micro-meteorological measurement of fluxes to conditions in which this turbulence is consistent across the layer and where the variability in vertical motion is not a result of waves or other structures that do not transfer mass vertically in the boundary layer. Of the flux-gradient methods considered, the approach using the “similarity” flux-gradient method resulted in the smallest difference to the IHF flux calculation, implying that the wind gradient and/or concentration gradient is not log-linear under stable conditions and therefore MOST cannot be applied.

5.2 Limitations to large-scale long-term emissions determination

Careful quality assurance of sonic anemometers provided sufficient accuracy, precision, and detection limits for flux determination and qualification in the stable boundary layer using a flux-gradient method. A primary limitation on the yield of valid flux measurements from these methods was instrument sensitivity; the precision of the sonic anemometers was sufficient to define the vertical gradient in wind speeds and turbulence parameters but the available FTIR spectrometer for the N₂O measurements did not routinely provide the necessary precision and detection limits to determine a statistically significant concentration gradient needed for flux determination. The use of a wider range in height may improve the flux estimate provided the lower measurement can be made closer to the surface. The FTIR also required internal optical adjustments which were dependent on the temperature environment and these adjustments significantly interrupted the measurement series. This was a first attempt at using flux-gradient methods in stable boundary layers with local perturbation partially averaged out by using open-path gas concentration measurements. A more sophisticated, longer term demonstration of the performance of trace gas flux determination by open-path gas measurements and flux-gradient approaches is needed to confirm applicability, ideally with spatially averaged turbulence measures matching the optical path of the gas measurement.
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