Validation of spectral sky radiance derived from all-sky camera images – a case study

K. Tohsing, M. Schrempf, S. Riechelmann, and G. Seckmeyer
Institut für Meteorologie und Klimatologie, Leibniz Universität Hannover, Herrenhäuser Straße 2, Hanover 30419, Germany

Correspondence to: K. Tohsing (korntip@su.ac.th)

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Abstract. Spectral sky radiance (380–760 nm) is derived from measurements with a hemispherical sky imager (HSI) system. The HSI consists of a commercial compact CCD (charge coupled device) camera equipped with a fish-eye lens and provides hemispherical sky images in three reference bands such as red, green and blue. To obtain the spectral sky radiance from these images, non-linear regression functions for various sky conditions have been derived. The camera-based spectral sky radiance was validated using spectral sky radiance measured with a CCD spectroradiometer. The spectral sky radiance for complete distribution over the hemisphere between both instruments deviates by less than 20 % at 500 nm for all sky conditions and for zenith angles less than 80°. The reconstructed spectra of the wavelengths 380–760 nm between both instruments at various directions deviate by less than 20 % for all sky conditions.

1 Introduction

The knowledge of spatial and spectral sky radiance distribution is important for many applications. For example, the sky radiance is used for studying the optical properties of mineral dust (Li et al., 2007) and bidirectional reflectance distributions (Deering and Eck, 1987). The optical thickness and the size distribution of aerosol were derived from the measured sky radiance using an inversion algorithm (Nakajima et al., 1996; Dubovik and King, 2000). The aerosol phase function and single scattering albedo can be determined from the sky radiance as well (Velmeulen et al., 2000). The spectral sky radiance is also used for the computation of the irradiance on surfaces, which is applied in design and performance investigations of spectral selective energy devices, such as photovoltaic (PV) systems (Steven and Unsworth, 1997; Hernández-András et al., 2001).

The variation of the sky radiance has been observed and analysed under different sky conditions by using several types of instruments (Dorno, 1911; Bener, 1963; Blumthaler et al., 1996; Ricchiazzi et al., 2000; Huber et al., 2004). Wuttke and Seckmeyer (2006) and Wuttke et al. (2006) performed spectral sky radiance measurements over the snow-covered surface in Antarctic environments in order to investigate the impact of high snow albedo on the sky radiance. A recent study by Pissulla et al. (2009) presented an intercomparison of spectral radiance measurements in the UV and visible wavelengths with high spectral resolution. These measurements were conducted by using five different instruments from three locations. The deviation of the measured spectral sky radiance varied between 3 and 35 % depending on the wavelength, location and the instruments.

Most of these spectral radiance observations have been compared with the results from a radiative transfer model. These comparisons were mostly under cloud-free conditions and under partly cloudy conditions. However, the equipment for measuring spectral radiance distributions is relatively non-mobile and expensive, which leads to insufficient spectral radiance data. Therefore, some researchers have applied all-sky images to determine the spectral sky radiance, which has great benefits in terms of acquisition time, mobility and cost.

The development of all-sky imagery for ground-based sky radiance observations has taken over a century. Voss and Zibordi (1989) presented the sky radiance distribution performed by the electro-optics fisheye radiance distribution camera system (RADS) and validated with radiance data from a hand-held contrast reduction meter. The sky radiance
distribution from the same system was also compared with sky radiance simulations (Zibordi and Voss, 1989).

The whole-sky imager was developed for ground-based cloud and radiance measurements (Shields et al., 1998; Feister et al., 2000). The grey level of a monochromatic CCD (charge coupled device) camera has been used to derive the sky radiance distribution for the different sky conditions (Huo and Lu, 2009) and the gray values combined with the radiometric calibration have been applied to obtain the spectral radiance (Rossini and Krenzinger, 2007). The spectral skylight from images using a linear pseudo-inverse has been presented (López-Alvarez et al., 2008). Recent research by Román et al. (2012) investigated the spectral sky radiance at three effective wavelengths from hemispherical sky images. A matrix calibration described the relationship between the output signal of images and reference values of the simulated sky radiance were proposed. The camera-based radiance has been estimated and validated with the sun photometer. However, validation of the spectral sky radiance distribution for the whole hemisphere with an accurate instrument has not been performed. Furthermore, the matrix calibration applied in this work is only valid when the spectral response of the CCD sensor is linear.

In contrast to Román et al. (2012), we propose a method to obtain the spectral sky radiance distribution from all-sky images for the complete spectrum in the visible part (380–760 nm) using the non-linear regression technique. The instrumentation and the methods for retrieving the spectral radiance will be introduced in the next section, followed by spectral and spatial comparison of the sky radiance distributions derived by the hemispherical sky imager (HSI) system with the measured radiance distributions obtained by a CCD spectroradiometer.

2 Instruments and data

2.1 The hemispherical sky imager (HSI) system

The hemispherical sky imager (HSI) was designed and developed at the Institute of Meteorology and Climatology (IMuK), University of Hanover, Germany (52.39° N, 9.70° E, at 59 m a.s.l.). This system contains a Canon PowerShot G10 compact camera, equipped with a Dörr DHG fish-eye lens, providing an image with a field of view (FOV) of about 183° and encapsulated in a weather-proof housing for long-term outside operation. Hemispherical pictures can be taken and stored by the software every second. To keep the amount of storage low, an interval of 20 s is useful. More detailed descriptions of the HSI system are given in Tohsing et al. (2013). The camera has a CCD sensor with three channels such as red, green and blue. The spectral response of the camera channels has been investigated at IMuK laboratory by using a light source from the 1000 W lamp passed through a monochromator projected onto a reflectance plaque. At each wavelength images of the plaque were acquired and further analysed to obtain the sensor sensitivity. The resulting spectral response of the camera sensor used is shown in Fig. 1. The maximum responses of each channel are at the wavelengths of 602, 527 and 441 nm for the red, green and blue channel respectively.

2.2 The CCD Array spectroradiometer

A CCD spectroradiometer system based on a CCD array spectrometer (S2000, Ocean Optics Inc., Dunedin, USA) and a positioning unit (SkyScanner, Czibula and Grundmann, Berlin, Germany) (Czibula and Grundmann, 2002) is used for measuring the spectral sky radiance distribution. Similar spectrometers have been used to measure solar and artificial radiation in Ansko et al. (2008); Kouremeti et al. (2008); Kreuter and Blumthaler (2009). The system is capable of measuring spectral sky radiance with a spectral resolution of 2 nm between 300 and 800 nm covering the visible part of the spectrum. The entrance optics has a 5° FOV (Seckmeyer et al., 2010). The spectral sky radiance at a given zenith and azimuth angle is measured within five seconds. Based on earlier investigations with the main focus on the UV range, the estimated uncertainty of the spectral radiance measurements is between 5 and 10 %. The methodology for calibration of the CCD spectroradiometer, which is performed at the beginning of the measurement, is described in Pissulla et al. (2009) and has been applied to spectral radiance measurements in the visible range as explained in Seckmeyer et al. (2010). The effects of uncertainties on experimental integrals for the UV part have been described in Cordero et al. (2008) and further details on the extension to the visible range can be found in Wuttke and Seckmeyer (2006) and Wuttke et al. (2006).
Non-linear regression is used to determine a relationship between two data sets – namely, the measured spectral radiance from the CCD spectroradiometer and the signal from the three channels of the HSI image. In the regression process, the optimum correlation was acquired with a variety of independent variables and the predictor variables were selected (Lütjohann, 1970).

The following two data sets were used in the training of the regression model for cloud-free condition. The first data set contains spectral sky radiance measurements, conducted with the CCD spectroradiometer in the wavelength range from 380 to 760 nm on 28 October 2012 from 12:00 to 16:00 UTC. The second data set consists of the signal counts of the three reference bands measured by the HSI system also on 28 October 2012, which have a maximum spectral response at the wavelength of 441 nm for the blue channel, 527 nm for the green channel and 602 nm for the red channel. In this case, the spectral direct radiance from the CCD spectroradiometer as well as the counts from the HSI system at the circumsolar area or about 20° around the sun were excluded in the regression model.

At each wavelength (i.e. each regression equation), the measured spectral sky radiance was treated as a function of the signal of red or green or blue counts, which range from 0 to 255 counts. Therefore, there are three non-linear regression equations for each wavelength and 1143 regressions for the complete spectrum. For different camera settings such as exposure time or aperture and due to the non-linear relationship between those settings and the count values different regression equations must be computed. In this work, the regression was performed for an exposure time of 1/1000 s, an ISO number (defined as sensitivity of a camera to incoming light) of 80 and an aperture of f/40. The results of the non-linear regression equations and the selection of those equations for each wavelength is presented in Sect. 4.1.

For the case of cloudy sky conditions, the regression was performed for the training data set on 23 October 2012 from 06:00 to 16:00 UTC measured by the CCD spectroradiometer and the HSI system. Except for the different training data set, the same method as described for the cloud-free condition was used. The reason for two training data sets (cloud-free and cloudy) is due to the high sensitivity of the HSI channel to cloud cover. The maximum values can reach 255 counts for bright clouds, whereas blue sky has at most about 120 counts. The use of one and the same training data set for

### Table 1. Measuring description of the CCD spectroradiometer and the HSI system for spectral sky radiance reproduction.

<table>
<thead>
<tr>
<th>Date</th>
<th>Hour measuring (UTC)</th>
<th>Sky conditions</th>
<th>Purpose</th>
</tr>
</thead>
<tbody>
<tr>
<td>19 Oct 2012</td>
<td>05:30–17:27</td>
<td>Partly cloudy</td>
<td>Validation</td>
</tr>
<tr>
<td>20 Oct 2012</td>
<td>05:30–16:44</td>
<td>Partly cloudy</td>
<td>Validation</td>
</tr>
<tr>
<td>21 Oct 2012</td>
<td>10:23–17:21</td>
<td>Cloud-free</td>
<td>Validation</td>
</tr>
<tr>
<td>22 Oct 2012</td>
<td>07:17–15:23</td>
<td>Overcast</td>
<td>Validation</td>
</tr>
<tr>
<td>23 Oct 2012</td>
<td>06:30–16:21</td>
<td>Overcast</td>
<td>Training</td>
</tr>
<tr>
<td>26 Oct 2012</td>
<td>05:30–17:20</td>
<td>Partly cloudy</td>
<td>Validation</td>
</tr>
<tr>
<td>28 Oct 2012</td>
<td>12:41–16:00</td>
<td>Cloud-free</td>
<td>Training</td>
</tr>
</tbody>
</table>
both conditions would lead to great deviation in the spectral radiance reconstruction.

Under intermediate sky, the FOV of some scanning points is not completely filled with either clouds or blue sky, as shown in Fig. 6d. In these cases, it is quite difficult to decide whether the cloud-free or cloudy sky regression model is more suitable. Therefore, the ratio of the count values of the red and blue channel (called sky index) was investigated to separate blue sky and white clouds (Yamashita et al., 2004). The sky index is expressed as

$$\text{Sky Index} = \frac{B - R}{B + R},$$

(1)

where $B$ is the count value of the blue channel and $R$ the count value of the red channel of the HSI system.

Eventually, all pixels of each scanning point were averaged to gain one representative sky index. The investigations showed that an average of sky index greater than 0.25 indicates blue sky. Thus, for these values, the cloud-free regression model will be applied for the spectral reconstruction, otherwise the sky element is covered by clouds.

A major challenge of this regression technique is that the collinearity between the predictor variables, which creates the regression relationship, is very specific to the training data set from which they are derived. Therefore, it would be unsuccessful to apply the same coefficients to other data set without a test of their suitability. Moreover, the training data set contains solar zenith angles 60–90° due to the fact that the measurements have been performed in wintertime. For the validation of the spectra reproduction method, the spectral radiance was calculated for an independent image data set from the HSI system during one week of the campaign acquired under different sky conditions as shown in Table 1. A discrepancy between the spectral sky radiance from the HSI system and the CCD spectroradiometer is presented as a ratio and also in terms of mean bias difference (MBD) and root mean square difference (RMSD). MBD is determined (Iqbal, 1983) by

$$\text{MBD} = \frac{1}{N} \sum_{i=1}^{N} \frac{(R_{\text{cam}} - R_{\text{mea}})}{R_{\text{mea}}} \times 100\%,$$

(2)

where $R_{\text{cam}}$ is the sky radiance derived from the HSI system, $R_{\text{mea}}$ is the measured sky radiance from the CCD spectroradiometer, $R_{\text{mea}}$ is the averaged sky radiance obtained from the CCD spectroradiometer and $N$ is the number of measurement data. The RMSD measures the variation between the computed values and the measured values. RMSD is expressed as follows (Iqbal, 1983):

$$\text{RMSD} = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (R_{\text{cam}} - R_{\text{mea}})^2} \times 100\%,$$

(3)

The results of the comparison between camera-based and measured spectral sky radiance are presented in Sects. 4.2 and 4.3.

4 Results

4.1 Non-linear regression model

The synchronized data sets collected on 23 and 28 October 2012 by the CCD spectroradiometer and the HSI system were used as training data sets to determine the non-linear regression equations. Figure 2 shows the non-linear regression fitted by a third-degree polynomial and the correlation coefficient ($R^2$) at the wavelength 500 nm for the three channels. The resulting plot in Fig. 3 presents the variation of the correlation coefficients of the training data for cloud-free sky on 28 October 2012 (left) and for cloudy sky on 23 October 2012 (right) plotted against the visible wavelength. For blue sky, the best correlation coefficients are at the centre of each band, which has a correlation coefficient of $R^2 > 0.95$ and the correlation coefficients of each channel vary with the wavelength that corresponds to the camera sensor response. The coefficients for cloud-free data of the red channel vary mostly in the region around 680–760 nm due to water absorption lines (Liou, 2002). In the case of cloudiness (see Fig. 3 right), there are variations of the correlation coefficients at wavelength less than 400 nm due to the absorption by ozone and in the 680–760 nm wavelength range, otherwise the correlation coefficients are quite constant ranging from about 0.85 to 0.92.

Therefore, the general equations of the non-linear regression models for each wavelength ($\lambda$) can be expressed by the following equations:

$$L_{\text{cam},r} = a_{0,\lambda} + a_{1,\lambda} R + a_{2,\lambda} R^2 + a_{3,\lambda} R^3$$

(4)

$$L_{\text{cam},g} = b_{0,\lambda} + b_{1,\lambda} G + b_{2,\lambda} G^2 + b_{3,\lambda} G^3$$

(5)

$$L_{\text{cam},b} = c_{0,\lambda} + c_{1,\lambda} B + c_{2,\lambda} B^2 + c_{3,\lambda} B^3$$

(6)

where $L_{\text{cam},r}$, $L_{\text{cam},g}$, $L_{\text{cam},b}$ are the sky radiance values obtained from the red, green and blue channels of the images.
4.2 Comparison of spectral radiance distribution at 500 nm from CCD spectroradiometer and HSI system

Examples of the spectral sky radiance at 500 nm for the whole hemisphere measured with the CCD spectroradiometer are compared with the spectral radiance from the HSI images for different sky conditions as shown in Figs. 4–6. Figure 4 shows the measurement and the comparison for cloud-free sky on 21 October 2012 at 13:12 UTC (scanning period is 13:12–13:24 UTC): (a) the measured spectral sky radiance from CCD spectroradiometer and interpolated for the whole sky (b) the spectral radiance distribution calculated from the HSI system, (c) the ratio between the camera-based and measured spectral sky radiance comparison point by point (no interpolation) and (d) 113 points of the synchronized HSI image reconstructed from about 35 images depending on the scanning time. The size of the illustrated scan points in Fig. 4d corresponds to the 5° FOV of the CCD spectroradiometer. Although the FOV of the scanning pattern is 5° (see d), the scanning points showing the ratio are plotted with a FOV of 10° for clarity of the presentation. The synchronized HSI image showing the 5° FOV pattern of the scanning points from the CCD spectroradiometer is illustrated in (d).

A rim at the horizon with higher values of spectral sky radiance can be observed, in contrast to the spectral sky radiance at the zenith. For the spectral sky radiance distribution, in general, the brightness of the horizon which is dominated by the Rayleigh scattering (Liou, 2002) increases with increasing wavelength and can clearly be observed in the measurements with the CCD spectroradiometer. From the results of the spectral sky radiance derived from the HSI system, the horizon brightening could not be identified at short wavelengths (400 nm) but could be distinctly observed at longer wavelengths (600 nm), which is not shown in the plots. The variation of the spectral sky radiance distribution at the wavelength 500 nm deviates by up to 10% for the whole hemisphere excluding the circumsolar region as shown in the ratio plot of Fig. 4c.

Figure 5 shows the comparison of the spectral sky radiance for the whole hemisphere for overcast sky conditions observed on 22 October 2012 at 09:29 UTC (scanning period, 09:29–09:41 UTC). The camera-based spectral radiance agrees well with the measured spectral sky radiance with a deviation up to 5% for zenith angles less than 80°. The result of this comparison can be seen in the ratio plot (Fig. 5c). The spectral radiance for zenith angles greater than 80° were not considered due to obstructions at the horizon.
The validation for partly cloudy sky, measured on 26 October 2012 at 12:01 UTC (scanning period, 12:01–12:13 UTC), is presented in Fig. 6. Most of the sky elements with a zenith angle greater than 50° were covered by clouds, while the zenithal area was cloudless. The sky index was determined and applied for separating blue sky and cloudy areas.

The comparison shows that the spectral radiance distribution of the blue sky at the zenith derived by the HSI system agrees well with the measurement with a deviation up to 10%. The same deviation is observed at scanning points that are fully covered by clouds. If scanning points are covered by a small degree by clouds, the HSI system overestimates the spectral sky radiance. In this case the deviation is less than 20%. However, the spectral sky radiance of bright clouds is overestimated by the HSI system.

The values of the MBD and RMSD of the compared sky radiance measurements for the wavelengths of 400, 500 and 600 nm during the measurement campaign under different sky conditions are summarized in Table 2. The HSI system tends to underestimate the spectral sky radiance with respect to the CCD spectroradiometer as presented by the MBD. The MBD and the RMSD of the spectral sky radiance in the case of partly cloudy sky between both instruments were found to be higher than for completely cloud-free and overcast skies.

4.3 Comparison of spectral radiance from CCD spectroradiometer and HSI system for the visible spectrum

The spectral sky radiance obtained for the whole visible spectrum of the wavelength from 380 to 760 nm by the HSI system was compared with the measurements of the three different sky conditions mentioned in Sect. 4.2. For each sky condition, two points of the scan pattern were chosen to represent the spectral validation.

In Fig. 7 the reconstructed spectra from 21 October 2012 at 13:12 UTC for the zenith angles of 36° and 72° and azimuth angles of 0° and 105° are illustrated. The validation shows that the camera-based spectral sky radiance agrees well with the spectral radiance from the CCD spectroradiometer and has a deviation of less than 10% in the 380 to 700 nm wavelength range as shown in the ratio plots of Fig. 7. For wavelengths greater than 700 nm the deviation can be up to 30% and could be caused by the absorption band of the water vapour (Liou, 2002) and the detection threshold of the CCD spectroradiometer in this wavelength region.

Figure 8 shows the radiance spectra for the overcast situation observed on 22 October 2012 at 09:29 UTC at the zenith and the scan point with the zenith angle of 48° and the...
azimuth angle of 202°. The spectral radiance from the HSI image agrees very well with the measured spectral zenith radiance from the CCD spectroradiometer with a deviation of less than 10% in the visible spectrum.

As shown in Fig. 9, the radiance spectra were also determined by the HSI system for a broken cloud condition observed on 26 October 2012 at 12:01 UTC. The scanning point with the zenith angle of 48° and the azimuth angle of 67°, shown in the upper panel, is covered up to one half with clouds. The sky index was found to be close to 0.22. Therefore, the regression model for cloudy conditions was selected. The resulting value from the HSI system is slightly higher than from the CCD spectroradiometer but the deviation is still within 10%. In the lower panel, the plot of the scanning point with the zenith angle of 60° and the azimuth angle of 162°, which was fully covered by cumulus clouds, is shown. The values of spectral sky radiance determined by the HSI system were smaller than the measured spectral radiance, with a deviation of up to 20% for wavelengths less than 700 nm. For wavelengths greater than 700 nm the deviation can increase up to 40% around the water absorption band. The deviation between the camera-based spectral radiance by

Figure 7. Spectral radiance measured on 21 October 2012 at 13:12 UTC by the CCD spectroradiometer and the HSI system for the scanning points with azimuth and zenith angles of 0° and 36° (upper panel) and 105° and 72° (lower panel). The ratio between the measured and computed spectral radiance is shown on the right.

Figure 8. Spectral radiance on 22 October 2012 at 09:29 UTC measured by the CCD spectroradiometer and the HSI system at the zenith (upper panel) and for azimuth angle of 202°, zenith angle of 48° (lower panel). The ratio between the measured and computed spectral radiance is shown on the right.
the HSI system and the measured spectral radiance from the spectroradiometer for all directions and zenith angles (entire hemisphere excepting the sun position) was up to 20% for wavelengths less than 700 nm. Sample results can be found in Sect. 4.2 for the wavelength of 500 nm. For wavelengths greater than 700 nm, the deviation can be up to 40% when some parts of scanning point were covered by clouds. Due to Mie scattering, the maximum radiance during cloudy situations is shifted from 400 nm for a cloud-free sky (Fig. 7, left upper panel) to 450 nm (Fig. 8, left upper panel) as described in Lenoble (1993). The shift of the radiance maximum to longer wavelengths was observed and investigated at different locations (Pissulla et al., 2009; Seckmeyer et al., 1994; Wuttke and Seckmeyer, 2006).

### 5 Conclusions

A non-linear regression model derived from the relationship between measurements and signal counts of the red, green and blue channels of hemispherical sky images was developed to derive the spectral sky radiance in the visible spectrum. The optimum non-linear regression equation for each wavelength was selected by using a training data set and the correlation coefficients between predicted radiance of the training set and the radiance from the measurements. For the validation, the camera-based spectral sky radiance from RGB image data obtained from the regression equations for the validation, the camera-based spectral sky radiance from the HSI system and the measured spectral radiance from a CCD spectroradiometer.

The spectral sky radiance distribution for the whole hemisphere showed that the camera-based spectral sky radiance deviated from the sky radiance measured by the CCD spectroradiometer by less than 20% at 500 nm for all sky conditions and for zenith angle less than 80°. The comparison between the reconstructed visible spectra (380–760 nm) and the measured spectra with the CCD spectroradiometer also shows good agreement with a deviation of less than 20% for all sky conditions. From these investigations, it can be

Table 2. The MBD and RMSD of the spectral sky radiance measured by the HSI system and the CCD spectroradiometer on various days corresponding to the sky conditions shown in Table 1.

<table>
<thead>
<tr>
<th>Date</th>
<th>MBD (%)</th>
<th>RMSD (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>400 nm</td>
<td>500 nm</td>
</tr>
<tr>
<td>20 Oct 2012</td>
<td>−17.76</td>
<td>−15.22</td>
</tr>
<tr>
<td>22 Oct 2012</td>
<td>−3.09</td>
<td>−2.12</td>
</tr>
<tr>
<td>31 Oct 2012</td>
<td>−10.41</td>
<td>−7.40</td>
</tr>
</tbody>
</table>

Figure 9. Spectral radiance measured on 26 October 2012 at 12:01 UTC by the CCD spectroradiometer and the HSI system for the scanning points with the azimuth and zenith angle of 67° and 48° (upper panel) and for the azimuth and zenith angle of 162° and 60° (lower panel). The ratio between the measured and computed spectral radiance is shown on the right. The agreement is considered to be satisfactory.
K. Tohsing et al.: Validation of the spectral sky radiances

concluded that the HSI system can derive the spectral sky radiances from hemispherical sky images with reasonable accuracy and reliability.

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