Retrieval of ash properties from IASI measurements

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Abstract. A new optimal estimation algorithm for the retrieval of volcanic ash properties has been developed for use with the Infrared Atmospheric Sounding Interferometer (IASI). The retrieval method uses the wave number range 680–1200 cm⁻¹, which contains window channels, the CO₂ ν₂ band (used for the height retrieval), and the O₃ ν₃ band.

Assuming a single infinitely (geometrically) thin ash plume and combining this with the output from the radiative transfer model RTTOV, the retrieval algorithm produces the most probable values for the ash optical depth (AOD), particle effective radius, plume top height, and effective radiating temperature. A comprehensive uncertainty budget is obtained for each pixel. Improvements to the algorithm through the use of different measurement error covariance matrices are explored, comparing the results from a sensitivity study of the retrieval process using covariance matrices trained on either clear-sky or cloudy scenes. The result showed that, due to the smaller variance contained within it, the clear-sky covariance matrix is preferable. However, if the retrieval fails to pass the quality control tests, the cloudy covariance matrix is implemented.

The retrieval algorithm is applied to scenes from the Eyjafjallajökull eruption in 2010, and the retrieved parameters are compared to ancillary data sources. The ash optical depth gives a root mean square error (RMSE) difference of 0.46 when compared to retrievals from the MODerate-resolution Imaging Spectroradiometer (MODIS) instrument for all pixels and an improved RMSE of 0.2 for low optical depths (AOD < 0.1). Measurements from the Facility for Airborne Atmospheric Measurements (FAAM) and Deutsches Zentrum für Luft- und Raumfahrt e.V. (DLR) flight campaigns are used to verify the retrieved particle effective radius, with the retrieved distribution of sizes for the scene showing excellent consistency. Further, the plume top altitudes are compared to derived cloud-top altitudes from the Cloud-Aerosol Lidar with Orthogonal Polarization (CALIOP) instrument and show agreement with RMSE values of less than 1 km.

1 Introduction

The detection of volcanic ash and the retrieval of its properties have become a topic of increasing interest following the eruption of Eyjafjallajökull in 2010. Volcanoes are responsible for the emission of large quantities of aerosol particles and gases – such as H₂O, CO₂, and SO₂ – into the atmosphere. The particles created during a volcanic event are classified according to size, with the smaller solid particles (radii < 2 mm) referred to as volcanic ash (Schmid, 1981). These particles can have significant effects upon the Earth’s radiation balance, air quality, and the aviation industry – with the worst outcome in the latter case resulting in engine failure (Grainger et al., 2013; Casadevall, 1994). Through the analysis of spectral information from satellite infrared spectrometers (such as the Atmospheric Infrared Sounder, AIRS; the Tropospheric Emission Spectrometer, TES; and the Infrared Atmospheric Sounding Interferometer, IASI), the optical and physical properties of volcanic ash can be derived (e.g. the mass of ash contained within the plume), and these can be used to calculate the parameters most useful in ensuring safe air travel (Dubuison et al., 2014). Several different approaches have been applied to the infrared spectra of different volcanic plumes, including methods based upon optimal estimation (Clarisse et al., 2010; Francis et al.,...
2 IASI

IASI, on board the MetOp platforms, is a series of three identical Fourier transform spectrometers designed primarily to provide data to be assimilated for use in numerical weather prediction (NWP). The instrument is a Michelson interferometer covering the mid-infrared (IR) from 645 to 2760 cm$^{-1}$ (3.62–15.5 µm) with a spectral resolution of 0.5 cm$^{-1}$ (apodized) and a pixel diameter at nadir of 12 km. MetOp’s sun-synchronous polar orbit and IASI’s wide swath width mean that global coverage is achieved twice daily with the daytime descending node overpass at 09:30 local time for IASI-A (Simioni et al., 1997; Chalon et al., 2001; Hébert et al., 2004). Since aerosol fields have high spatial and temporal variability, regular views of the same area are essential to characterize plume evolutions. Therefore, IASI’s characteristics make it a very useful tool for the observation of larger aerosol particles (such as dust and volcanic ash). The work shown here uses IASI level 1c radiance data obtained from the British Atmospheric Data Centre (BADC) archive.

3 Retrieval method

3.1 Optimal estimation algorithm

An optimal estimation scheme has been developed to retrieve the properties of volcanic ash plumes. The method analyses the brightness temperature spectra from IASI to retrieve the following parameters: ash optical depth (at a reference wavelength of 550 nm), ash effective radius (µm), ash plume top height (km), and effective radiating temperature (K).

An ash detection method, based upon the trace gas detection method described by Walker et al. (2011) and applied to volcanic ash by Sears et al. (2013), flags IASI pixels for the presence of volcanic ash. The detection procedure looks for departures in a spectrum from an expected background covariance. An ensemble training set of IASI data, assumed to contain no extraordinary ash concentrations, is used to create a generalized error covariance matrix that contains the spectral variability caused by interfering trace species and clouds as well as the IASI instrument noise. A least-squares fit retrieval is carried out to retrieve the ash optical depth at three assumed altitudes: 400, 600, and 800 mb. The pixel is flagged if the ash optical depth at any of the altitudes passes a given threshold. In previous work, the presence of volcanic SO$_2$ has been used as a proxy for the location of volcanic ash; therefore, pixels are also flagged for SO$_2$ in the same manner as Carboni et al. (2012), and the retrieval is subsequently calculated for pixels that are flagged to contain either a positive ash or SO$_2$ signal. The ash and SO$_2$ flags are produced in near-real time, and the results are publicly available within 3 h of measurement at http://www.nrt-atmos.cemr.rl.ac.uk/.

For a detailed description of optimal estimation see Rodgers (2000), but essentially we define the measured spectra, y, and attempt to simulate it using the forward model,
\( \mathbf{F}(x, b) \):

\[ y = \mathbf{F}(x, b) + \epsilon, \quad (1) \]

where \( x \) is the state vector containing the parameters to be retrieved. All atmospheric properties needed by the forward model that are not retrieved are contained in \( b \), and \( \epsilon \) contains all the uncertainties associated with the retrieval.

The retrieval aims to find the most probable state of \( x \) by minimizing the cost function, \( \chi^2 \), given by

\[ \chi^2 = \left[ y - \mathbf{F}(x, b) \right]^T S_c^{-1} \left[ y - \mathbf{F}(x, b) \right] + [x - x_a]^T S_a^{-1} [x - x_a], \quad (2) \]

where \( x_a \) is the a priori value of the state vector, and \( S_c \) and \( S_a \) are the measurement and a priori error covariance matrices respectively.

In order to find the minimization point of Eq. (2), the Levenberg–Marquardt–Press method is implemented, which numerically iterates the retrieval until a convergence criterion is satisfied (a positive or negative change in the cost of 1) or a maximum number of iterations is reached (default is 10). In the former case the retrieval is considered to have converged; in the latter case, the retrieval is deemed to have failed and rejected. Full details of this implementation can be found in Rodgers (2000).

### 3.2 Assembling the error covariance matrix

The measurement error covariance matrix, \( S_c \), is built up from an ensemble of difference spectra, capturing the variability between the IASI data and the radiative transfer model calculations. Each of the spectra is the residual between an IASI measurement and a spectrum simulated using the forward model and co-located atmospheric profile data. Only scenes where there is confidence that no volcanic signatures are present are included. This creates a generalized error covariance matrix containing not just the instrumental noise but also the spectral variability due to any inability for the forward model to correctly simulate the IASI measurements, for example due to the presence of cloud, errors in the spectroscopy, or errors in the atmospheric profiles. Assuming that the state of such variables is of no interest (in this problem) and the spectral signal of these variables is orthogonal to the ash signal, including these spectral signatures within the error covariance means there is no need for them to be retrieved nor their variance to be accounted for in the forward model of the atmosphere, thus allowing the problem to be simplified. More specifically, the assumptions in this method allow the retrieval of the orthogonal component of the retrieval parameters.

The elements of the error covariance are calculated using

\[
S_c(i,j) = \left[ \left( y_j - \mathbf{F}(x_i) \right) - \left( y - \mathbf{F}(x) \right) \right]^T \left[ \left( y_j - \mathbf{F}(x_j) \right) - \left( y - \mathbf{F}(x) \right) \right],
\]

where \( (y - \mathbf{F}(x)) \) is the mean spectral difference between the measurement and a clear-sky simulation for each channel. The brightness temperature uncertainties are assumed to be normally distributed.

Given that the error covariance is relative to this mean residual, the input IASI spectrum to the retrieval must be adjusted to account for this bias. This produces a new cost function that must be minimized:

\[
\chi^2 = \left[ y - \mathbf{F}(x, b) - c \right]^T S_c^{-1} \left[ y - \mathbf{F}(x, b) - c \right] + [x - x_a]^T S_a^{-1} [x - x_a],
\]

where \( c \) is the mean residual.

Initially, when selecting the IASI scenes to include in the creation of the covariance matrix, only scenes from days with no known volcanic activity were used. However, this produces a covariance with a large variance due to the large impact the presence of cloud has upon the spectral region chosen for the retrieval, i.e. any transparent window channels. In cloudy scenes, this makes the retrieval possible as the variation due to cloud is accounted for and, because of the large variance, the retrieval is able to converge. However, for a clear-sky scene, including such large variances allows the retrieval to appear to converge, albeit with a large uncertainty. Therefore, separate covariance matrices have been produced using solely either clear-sky scenes or cloudy scenes, where a cloudy scene is deemed to be where the window channel brightness temperature differs by more than 5 K from the European Centre for Medium-Range Weather Forecasts (ECMWF) co-located surface temperature. These matrices shall henceforth be referred to as the “clear” and “cloudy” covariance matrices and can be seen in Fig. 1. In both instances the forward model assumes a clear-sky scene. Pictorial examples of the scenes each covariance applies to can be seen in Fig. 2. The clear-sky covariance also encompasses scenes for which there is a thin meteorological cloud beneath the plume that does not alter the window channel temperature significantly, whilst there is no covariance matrix that is able to cope with a thick meteorological cloud above the ash plume, meaning retrievals in these scenes are still challenging. The covariance used in scenes where meteorological cloud is at the same altitude as the ash plume will depend upon the optical thickness of the cloud, and the retrieved ash optical depth is expected to be an underestimate of the actual ash plume properties. Further challenges caused by the presence of ice in the ash plume due to the similarity in their spectral signatures are well known (Rose et al., 1995; Durant et al., 2008; Kylling, 2016). Some of their variability will have been captured in
the covariance matrices. However, if the ash particles have become coated in ice, the optical properties are changed and the retrieval may underestimate the quantity of ash. Further work will look to better distinguishing the ash and ice cloud signatures.

It must be noted that there are further error components that are not considered within the current covariance matrices that may be addressed in future work. These are the errors associated with the modelling of the plume, such as assuming a plane-parallel atmosphere, assuming that there is no leakage of radiation from the edges of the plume, assuming that the plume has only a single layer, and assuming the ash particles to be spherical and have a log-normal size distribution of fixed spread.

3.3 Forward model description

Due to the computational intensity of the retrieval algorithm the forward model used to simulate the atmospheric conditions must be chosen to achieve a practical speed; for this a fast radiative transfer model is needed. The chosen model to simulate clear-sky radiances (i.e. containing gaseous absorbers but not cloud or aerosol/ash) is RTTOV (Saunders et al., 1999; Hocking et al., 2014), and its output is combined with an ash layer using the same scheme as that for the Optimal Retrieval of Aerosol and Cloud (ORAC) algorithm; see Sect. 5.1.1.

Standard atmospheric profiles are assumed within the forward model, except for temperature, pressure, altitude, and water vapour. These profiles are obtained from ECMWF operational forecast data (European Centre for Medium-Range Weather Forecasts, 2012), available for every 6 h, and interpolated to the average time of the IASI orbit (or time of analysed section of orbit) to be processed and at the coordinates (latitude, longitude) of every IASI pixel. These profiles are then passed to the forward model. Future work may involve including the ECMWF ozone data as well. Despite little trace gas information being included and RTTOV using default standard atmospheric conditions for most absorbers, the use of the generalized error covariance will account for the variability of such species.

RTTOV provides the clear-sky top of atmosphere (TOA) radiance along with both upwelling and downwelling radiances at each altitude level. These can be used to formulate...
an overcast TOA radiance that includes a single layer of ash (or other broadband scatterer), which is assumed to be infinitely thin. Figure 3 shows schematically the interaction of the ash–atmosphere model. As per Thomas et al. (2009a), we define the following parameters to be

- $R_\text{al}^\uparrow$, the TOA clear-sky radiance;
- $R_\text{al}^\uparrow$, the TOA radiance associated with the atmosphere above the ash layers;
- $R_\text{bl}^\uparrow$, the upwelling radiance at the ash layer;
- $R_\text{al}^\downarrow$, the downwelling radiance at the ash layer;
- $T_\text{al}$, $T_\text{bl}$, the transmission of the atmosphere above and below the ash layer respectively;
- $T_1$, the transmittance of the ash layer;
- $B_s$, $B_\text{al}$, the Planck radiance of the surface and ash layer respectively;
- $\epsilon_s, \epsilon_1$, the emissivity of the surface and ash layer respectively;
- $\tau$, the reflectivity of the ash layer.

$R_\text{al}^\uparrow$, $R_\text{al}^\downarrow$, $R_\text{bl}^\downarrow$, $R_\text{al}^\text{atm}$ (the atmospheric contribution of $R_\text{bl}^\downarrow$), and $T_\text{al}$ are calculated efficiently within RTTOV. $R_\text{bl}^\downarrow$ must account for the contribution of both the surface and the atmosphere below the ash layer to the upwelling radiance by $R_\text{bl}^\downarrow = R_\text{bl}^\text{atm} + \epsilon_\text{bl} B_\text{bl} T_\text{bl}$, where the total atmospheric transmission, $T_\text{atm} = T_\text{bl} T_\text{al}$. The emissivity, reflectance, and transmittance of the ash layer are functions of the state vector elements, optical depth ($\tau$), effective radius ($r_{\text{eff}}$), and plume top height ($h$) as well as the observation geometry. Computational efficiency is optimized by pre-computing these properties of the ash layer using DISORT (discrete ordinate method for radiative transfer; Stamnes et al., 1988) and storing the results in look-up-tables (LUTs), which are linearly interpolated spectrally to the appropriate values. The spectral aerosol optical properties (extinction coefficient, single-scattering albedo and the phase function) for ash are calculated using Mie theory (Grainger et al. (2004); code available at http://eodg.atm.ox.ac.uk/MIE/) and external mixing. The ash particles are assumed to be spherical with a monomodal log-normal aerosol size distribution, which has been shown to be a suitable representation of the size distribution of airborne volcanic ash (Wohletz et al., 1989). The distribution is characterized by a spread of 2 (Wen and Rose, 1994b; Yu et al., 2002; Rybin et al., 2011; Pavolonis et al., 2013b), and the mode radius is translated to obtain different effective radii. The refractive index used in this paper is from measurements of ash from the Eyjafjallajökull eruption (Peters, 2010). These properties are calculated every 5 cm$^{-1}$ in the spectral range used by the retrieval, across a range of effective radii from 0.01 to 20 µm, to create the input for DISORT.

Ignoring multiple reflections between the layer and the surface, the “ash” TOA radiance, $R_\text{al}^\uparrow$, can be expressed as

$$R_\text{al}^\uparrow = R_\text{bl}^\downarrow T_\text{al} + B_1 \epsilon_1 T_\text{al} + R_\text{al}^\downarrow R_\text{al} + R_\text{al}^\uparrow,$$  

where the terms on the right-hand side correspond to, in order, the upwelling radiance below the ash layer transmitted by the layer and atmosphere above it, the emission from the ash layer, the reflected downwelling radiance above the ash layer, and the upwelling radiance contribution from the atmosphere above the ash layer.

### 4 Error analysis/sensitivity study

An advantage of the optimal estimation framework is it provides a rigorous estimation of the uncertainty in the retrieved state. The a posteriori error covariance matrix, $S_x$, can be written as

$$S_x = (K S_e^{-1} K + S_n^{-1})^{-1},$$

where $K$ is the Jacobian, which represents how the measurement spectrum is expected to change given a perturbation to the state. The diagonals of $S_x$ provide the expected variance on the retrieved state vector elements, and, hence, the square root of the diagonals give the uncertainty in each retrieved parameter. The optimal estimation retrieval produces the most probable values for ash optical depth, particle effective radius, plume top height, and effective radiating temperature, each with associated uncertainties. Further, from these values and an assumed ash density, the ash mass in the plume can be derived (see http://eodg.atm.ox.ac.uk/user/grainer/research/aerosols.pdf).

An uncertainty analysis was performed using synthetic spectra (adding an ash plume to a reference clear atmosphere) to assess the sensitivity of the retrieved parameters to variations in the state. In the simulations the ash optical depth at 550 nm varied between 0.01 and 10, and the plume...
Figure 4. The uncertainties in the retrieved parameters and the DFS available in the retrieval using the clear (first column) and cloudy (second column) covariance matrices, shown as a function of ash optical depth (horizontally) and plume top altitude (vertically). From the top, the rows exhibit the uncertainties in ash optical depth, effective radius, plume top altitude, effective radiating temperature, and available DFS. Any value higher than the colour bar scale is shown hatched.
top altitude lay between 1000 and 100 mb (~0–16 km). For the examples shown in Fig. 4 the effective radius and effective radiating temperature are held constant at 2 µm and 291 K respectively. (Simulations were also carried out varying these values, but they are not shown here). The a priori uncertainty estimates used were ±1 for the logarithm of ash optical depth, ±6 µm for effective radius, ±150 mb for altitude, and ±20 K for effective radiating temperature. The results show the uncertainties in the retrieved parameters and the degrees of freedom for signal (DFS) within the retrieval for different scenarios. The DFS is a figure of merit that expresses the information contained in a retrieval by compressing the information within the retrieval error covariance matrix into a single scalar quantity. Essentially, it provides the number of independent pieces of information available in an estimate of the state. All examples consider a “local” error covariance matrix, S_L, which is computed using spectra located at all longitudes within the latitude band, 30–60° N, above the Icelandic plume region, which is calculated as described in Sect. 3.2. The resultant uncertainties are shown for optimal estimation retrievals using both the clear and cloudy covariance matrices.

Using the clear covariance gives consistently larger DFS available for all combinations of parameters, with optically thick plumes at lower altitudes having nearly 0.5 DFS more than the results using the cloudy covariance. The impact of this difference in DFS can be seen in the uncertainty in effective radiating temperature, where the more optically thick plumes have a significantly larger uncertainty. Interestingly, and perhaps unexpectedly, the effective radiating temperature uncertainty improves when the ash layer is at the highest altitudes. This is due to the substantially larger amount of atmosphere below a plume at 16 km (as opposed to 8 km). This leads to an increase in the fraction of the total radiance across the window regions contributed by the atmosphere below the plume and, conversely, a decrease in the fraction of the total radiance that comes from the emission of the plume itself. It is also known that discerning ash plumes from meteorological cloud is challenging when the temperature contrast with the surface is very small (Prata and Grant, 2001). Additionally, the region of low effective radiating temperature uncertainty (high-altitude and optically thick plume) coincides with the region with the lowest plume top altitude uncertainty. Essentially, the more accurately we are able to retrieve the height of the plume, the more information that is available to improve the effective radiating temperature estimate. This behaviour has been seen in several other instances, such as Ackerman (1997) and the retrieval of SO_2 by Carboni et al. (2012).

The retrieved altitude uncertainty is typically < 1 km, with the uncertainty for optically thick plumes (AOD > 1) reducing to < 0.5 km when using the clear covariance. However, as the plume becomes optically thinner and less information is available, the retrieval tends towards the a priori value and the uncertainty estimate increases to become the a priori uncertainty.

For both ash optical depth and effective radius, the associated uncertainties have a similar pattern and are significantly lower for large values of optical depth. The smallest uncertainties occur for high-altitude, optically thick plumes, similar to both plume top height and effective radiating temperature, as this is where the largest number of DFS is available. In contrast to the uncertainty in plume top altitude, the estimated uncertainties decrease as the height of the plume increases, with a maximum expected uncertainty near the surface. This is most apparent at AOD < 0.5, with the maximum uncertainty occurring at the surface for the most optically thin plumes. At AOD < 0.1 it is observed that the uncertainty in effective radius and AOD reach 100 % and even higher in the latter case. Therefore, retrieval outputs of AOD values this small should be handled with caution.

The overarching behaviour of the expected uncertainty produced using both the clear and cloudy covariance matrices is the same, with the clear covariance producing consistently smaller uncertainty. It must be noted that this sensitivity study was carried out assuming a clear atmosphere with no clouds (except for the volcanic ash plume), and therefore the clear covariance is expected to perform better due to the smaller variance it contains. If used for a cloudy scene, this smaller variance gives rise to the potential for a retrieval to have a high cost or fail to converge entirely, whereas the larger variance of the cloudy covariance matrix can account for the cloud beneath the plume and produce a better retrieval.

Ideally, the clear covariance matrix would be used for plume scenes where there is no meteorological cloud, and the cloudy covariance matrix would be used for scenes where meteorological cloud is detected. Cloud clearing of this manner is challenging and infeasible. Instead, a criterion is currently applied to the retrieval whereby it must pass a set of quality control tests. These ensure the output is sensible and realistic (e.g. the plume top altitude is not below the surface or the effective radius negative) but also only consider the retrieval a success if it converges within 10 iterations and the normalized cost is below a specified threshold (default is 2). Consequently, the retrieval is first carried out using the clear covariance matrix, and then, if it fails to pass the quality control tests, the retrieval is further carried out using the cloudy covariance matrix. If the retrieval again fails to pass the quality control tests, it is discarded and deemed a failed retrieval.

5 Validation of retrieved parameters

An example of the retrieved plume properties and their associated uncertainties is shown in Fig. 5 for the morning of 9 May 2010 during the eruption of Eyjafjallajökull. This scene demonstrates the spatial consistency of the retrieval output, and the histograms of the plume properties also show that the output values are distinctly moving away from the a priori values with the modal values for AOD, effective radius, and height equaling 0.15, 1 µm, and 3.5 km respectively (the
Figure 5. Example retrieval output from 9 May 2010 during the eruption of Eyjafjallajökull. The left-hand column presents the retrieved parameters: ash optical depth, effective radius, and height. The centre column shows a histogram of the respective retrieved values with the a priori value indicated by the red dotted line, and the right-hand column contains the associated uncertainties for each parameter.

a priori values are 0.3, 2 µm, and 4.2 km respectively). The associated uncertainties are also promising, especially for the height product, which shows uncertainty of ~1 km – the same as in the sensitivity study for synthetic spectra. This plume is optically thin with typical AOD values of 0.15–0.2. In the sensitivity study, it was shown that large uncertainties were expected at low AOD. This is the case here for some pixels; however, the modal uncertainty of ~0.1 is less than the spread of retrieved values (~0.2). The same behaviour is also observed in the effective radius and height products. In the following sections, the retrieval outputs are compared to ancillary data sources to ensure consistency with existing products. Further validation of this algorithm can be seen in Balis et al. (2016) and Corradini et al. (2016).

5.1 Aerosol optical depth: comparison to MODIS

5.1.1 MODIS retrieval method

MODIS instruments reside aboard the sun-synchronous orbiting NASA Terra (launched May 2002) and NASA Aqua (launched December 1999) satellites. Terra orbits at a 705 km altitude, with a period of 98.8 min, an inclination of 98.2°, and a 10:30 equatorial crossing time on the descending node. Aqua orbits at a 705 km altitude, with a period of 98.4 min, an inclination of 98.1°, and a 13:30 equatorial crossing time on the descending node. For this study we use Terra observations which are closer in time to IASI’s 09:30 equatorial crossing time aboard Metop-A. With a cross-track swath of 2330 km MODIS provides global coverage nearly every day. It has 36 bands from 0.41 to 15 µm at 250 m (0.645 and 0.858 µm), 500 m (5 bands from 0.469 and 2.130 µm), and 1 km (29 bands from 3.750 to 14.235 µm) spatial resolutions.
For this study we use products derived from measurements aggregated to 1 km for all bands.

ORAC uses radiances measured from satellite-based imaging radiometers, including MODIS, to retrieve aerosol, cloud, volcanic ash, and surface properties. The retrieval algorithm is based on a long heritage of optimal estimation based on the work of Rodgers (2000) and authors cited within and has been applied by several researchers for aerosol and cloud retrievals (Thomas et al., 2009b; Sayer et al., 2011; Poulsen et al., 2012) and more recently for volcanic ash retrievals (McGarragh et al., 2016). For MODIS ash retrievals ORAC uses measurements of solar reflectance in bands 1, 2, and 6 (0.65, 0.86, and 1.64 µm respectively) and thermal brightness temperature in bands 20, 27, 28, 29, 31, 32, 33, 34, 35, and 36 (3.8, 6.7, 7.3, 8.6, 11.0, 12.0, 13.3, 13.6, 13.9, and 14.2 µm respectively). The primary retrieval parameters include ash optical thickness at 550 nm, effective radius of a log-normal ash particle size distribution, ash plume top pressure, and effective radiating temperature. Parameters derived from these include the ash optical thickness at 11 µm, derived from the optical thickness at 550 nm and the effective radius; the ash plume top height and temperature, derived from the optical thickness at 550 nm and the effective radius; and an assumed ash density of 2.6 g cm$^{-3}$ (Neal et al., 1994).

The ash particles are assumed to be spherical with a log-normal size distribution, and the size distribution averaged spectral optical properties (extinction coefficient, single-scattering albedo, and phase function) are calculated using Mie theory. Since the width of the distribution is not a retrieval parameter, it must be assumed, and a standard deviation of 2.0 is the value adopted for the ORAC retrieval. The complex index of refraction must also be assumed for which we use values measured from Eyjafjallajökull ash samples (Peters, 2010). These properties are the same as those assumed in the IASI retrieval.

The ash optical properties are further used as input to the plane-parallel radiative transfer solver DISORT to compute scalar spectral reflectance, transmission, and emission operators used in a “fast” forward model, details of which are described in McGarragh et al. (2016) and stored in LUTs as a function of the retrieved 0.55 µm optical thickness and effective radius, in addition to the solar and satellite geometry. The optical thickness at 11 µm is obtained directly from the ratio of the extinction coefficient at 11 µm to that at 0.55 µm. The ash plume is assumed to be infinitely thin geometrically, allowing for a full decoupling of the ash radiative transfer from that of the clear-sky for which the transmittance and emission are computed with RTTOV from meteorological pressure, temperature, humidity, and ozone profiles from the ECMWF ERA-Interim reanalysis product (Dee et al., 2011). Molecular (Rayleigh) scattering is computed according to Bates (1984) from the pressure and temperature profiles. Finally, the surface is characterized with a bidirectional reflectance distribution function (BRDF) for both land (Schaaf et al., 2002) and ocean (Sayer et al., 2010). Specific details regarding the sources of uncertainty are discussed in Thomas et al. (2009b), Sayer et al. (2011), and McGarragh et al. (2016).

5.1.2 Co-locating the data

IASI and MODIS have very different fields of view, and, hence, they must be co-located in order for a comparison to be carried out. The number of MODIS retrievals is far greater than that for IASI due to its better spatial resolution along the track. In order to compare the results, the MODIS data are aggregated onto the IASI resolution; i.e. all MODIS pixels within 6 km of the IASI pixel centre are used to formulate the average. Co-location is assumed if the IASI measurements and the MODIS measurements lie within 50 km and 1 h of each other.

5.1.3 Results

A comparison of the AOD at 11 µm retrieved by both the IASI and MODIS algorithms is shown in Fig. 6. Although the retrievals provide their AOD output at 550 nm, these values are obtained by spectral extrapolation, and the value of AOD at 11 µm is more appropriate for comparison as it lies within the actual wave number range for both instruments. The data shown are from the Eyjafjallajökull eruption in 2010, and only the retrievals that pass the imposed quality control measures for both algorithms are shown (73 coincidences). These measures ensure the output is sensible and realistic (e.g. the plume top altitude is not below the surface or the effective radius negative), and the normalized cost function must be below an imposed threshold of 2 for IASI and 5 for MODIS. A further criterion was imposed upon the MODIS data that all of the data points averaged onto the IASI pixel resolution must be flagged as ash by the MODIS algorithm for the aggregated pixel to be used in the comparison. This is to ensure that we are comparing like with like.

Reasonable correlation, $r = 0.47$, is observed between the two instruments with an root mean square error (RMSE) value of 0.66. It is visually clear that there is a grouping of pixels where MODIS overestimates the value of AOD compared to IASI. These coincide with the higher MODIS cost values and largest pixel variability (shown as error bars in Fig. 6) at AOD $> 1$. By removing these pixels, the correlation is much improved to $r = 0.64$. This is especially true for lower values of AOD, where the RMSE reduces to 0.2 (for AOD $< 1$) and 0.17 (for AOD $< 0.5$). As the AOD increases, the spread of the data also increases with the tendency for MODIS to see a higher AOD than IASI. However, there is a time difference between the data points, and therefore the instruments may not be viewing the same part of the plume, despite attempts to minimize this. Hence, perfect agreement is not expected, and the correlation seen is extremely encouraging.
Figure 6. Comparison of AOD at 11 µm retrieved from IASI and MODIS during the Eyjafjallajökull eruption. The error bars show the associated IASI retrieval error and the standard deviation of the MODIS retrievals that were aggregated across the IASI pixel.

5.2 Effective radius: comparison to aircraft measurements

5.2.1 Aircraft description

Immediately following the Eyjafjallajökull eruption in 2010, it became clear that aircraft measurements (both in situ and remote sounding) were needed in order to validate the ash dispersion forecasts. Two of the European aircraft deployed were the UK’s BAe-146 FAAM aircraft (http://www.faam.ac.uk) and Germany’s DLR Falcon aircraft (http://www.dlr.de). These aircraft are described in great detail elsewhere (see Marenco et al. (2011), Turnbull et al. (2012), and Newman et al. (2012) for FAAM aircraft; Schumann et al. (2011) for DLR aircraft), and therefore only a brief description is given here.

On board the FAAM aircraft were instruments capable of taking in situ and remotely sounded measurements. The in situ observations come from two wing-mounted optical particle counters: a passive cavity aerosol spectrometer probe for particles with size distributions of diameter 0.1–3 µm and a cloud and aerosol spectrometer for particles of diameter 0.6–50 µm. Essentially these equate to fine- and coarse-mode aerosol respectively. The principal remotely sounded observations came from the on-board lidar instrument: an ALS450 elastic backscatter lidar mounted to view in the nadir, which operates at a wavelength of 355 nm and has a footprint ranging from 7 to 11 km.

The DLR aircraft used the same instruments as the FAAM aircraft; however, the assumptions made in the calculation of the size distributions were different. Values for the optical properties (refractive index and shape) of the particles must be assumed as the response of the detectors is dependent upon these as well as the size (Turnbull et al., 2012). The DLR results assume spherical particles, whereas the FAAM aircraft provide results for both spherical and irregular particles, with an additional result assuming the refractive indices of the DLR model, showing how the differing assumptions affect the results.

5.2.2 Results

Turnbull et al. (2012) provide in situ measurements of the Eyjafjallajökull volcanic ash cloud on 17 May 2010 from both the FAAM and DLR flight campaigns. Despite no actual overlap in the flight paths of the aircraft, a worthwhile comparison is still possible, and here we further compare to the IASI retrievals on the same day. Values for the geometric mean diameter and standard deviation of the particle size distribution are given from both aircraft for both the fine and coarse particle modes. In order to compare these results to the retrieved IASI parameters, they must be converted into number-weighted mean radius, \( r_N \), by

\[
 r_N = \frac{D_g}{2} e^{-3\sigma^2},
\]

where \( D_g \) is the geometric mean diameter by volume and \( \sigma \) is the logarithm of the geometric standard deviation, \( S \). Further, due to IASI having sensitivity to both the fine and coarse modes, they are combined to calculate the effective radius, \( r_{\text{eff}} \), using

\[
 r_{\text{eff}} = \frac{\sum m_i \exp \left[ 2 \log r_{N,i} + 2\sigma_i^2 \right]}{\sum m_i \exp \left[ 2 \log r_{N,i} + 2\sigma_i^2 \right]},
\]

where the mixing ratios \( m_i \) are the relative weight of each mode and a log-normal distribution is assumed. The size distributions obtained from the aircraft measurements can be seen in Table 1. Further, a histogram of the effective radius retrieved by IASI across all scenes containing the volcanic ash plume on 17 May can be seen in Fig. 7.

The values for the particle effective radius vary due to differing assumptions made in the calculations. The assumed type of size distribution in the retrieval and assumed shape in the aircraft calculations can impact the expected effective radius. The distribution of retrieved effective radius from IASI measurements is consistent with the values from the aircraft measurements, although slightly smaller. This is expected to be due, in part, to the sensitivities of the different instruments to different particle sizes, as well as due to the IASI histogram including the full extent of the plume and, therefore, including regions where the larger particles have been deposited out of the plume.

5.3 Plume altitude: comparisons to CALIOP

5.3.1 CALIOP

CALIOP is the primary instrument on board the Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observa-
Table 1. The parameters observed by aircraft on 17 May 2010 (geometric mean diameter by volume, geometric standard deviation, and relative weight by mass, taken from Turnbull et al., 2012) and the effective radius calculated from the size distributions. The mode effective radius measured for the entire ash plume observed by IASI is also shown.

<table>
<thead>
<tr>
<th>Measurement source</th>
<th>Geometric mean diameter [µm]</th>
<th>Standard deviation [µm]</th>
<th>Relative weight</th>
<th>Effective radius [µm]</th>
</tr>
</thead>
<tbody>
<tr>
<td>FAAM irregulars</td>
<td>Fine mode 0.20</td>
<td>1.4</td>
<td>0.035</td>
<td>0.870</td>
</tr>
<tr>
<td></td>
<td>Coarse mode 3.6</td>
<td>1.8</td>
<td>0.965</td>
<td></td>
</tr>
<tr>
<td>FAAM spheres</td>
<td>Fine mode 0.2</td>
<td>1.4</td>
<td>0.028</td>
<td>0.977</td>
</tr>
<tr>
<td></td>
<td>Coarse mode 4.0</td>
<td>1.85</td>
<td>0.972</td>
<td></td>
</tr>
<tr>
<td>FAAM using DLR refractive indices</td>
<td>Fine mode 0.18</td>
<td>1.35</td>
<td>0.015</td>
<td>1.186</td>
</tr>
<tr>
<td></td>
<td>Coarse mode 4.5</td>
<td>1.9</td>
<td>0.985</td>
<td></td>
</tr>
<tr>
<td>DLR spheres</td>
<td>Fine mode 0.12</td>
<td>1.6</td>
<td>0.020</td>
<td>1.126</td>
</tr>
<tr>
<td></td>
<td>Coarse mode 9.6</td>
<td>2.5</td>
<td>0.980</td>
<td></td>
</tr>
<tr>
<td>IASI retrieval</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>0.75</td>
</tr>
</tbody>
</table>

Figure 7. A histogram of the effective radius retrieved in the IASI scenes on 17 May 2010.

5.3.2 Co-locating the data

Given the very differing footprints of IASI and CALIOP, they must be co-located in order to allow comparison. The frequency of IASI retrievals is far greater than that for CALIOP; however, CALIOP has far greater spatial resolution along the track. CALIOP observations of volcanic plumes have been identified using Spinning Enhanced Visible and Infrared Imager (SEVIRI) false-colour images based on the infrared channels at 8.7, 11, and 12 µm (Thomas and Siddans, 2015), where the backscatter profiles have been averaged vertically to a resolution of 250 m. In order to compare the results, the CALIOP data are smoothed onto the IASI resolution; i.e. all pixels become an average of the pixels within a 12 km spread. Co-location is assumed if the IASI measurements and the CALIOP measurements lie within 50 km and 1.5 h of each other. Where multiple CALIOP pixels satisfy this criterion for a selected IASI pixel, the CALIOP pixel closest in distance is chosen, under the assumption that the conditions will not vary much over the time period.

CALIOP produces atmospheric backscatter profiles for every pixel. However, the quantity required for validation is the cloud top height of the volcanic plume as this is the comparable ash property retrieved from IASI. Initially, the mean backscatter above 15 km is calculated for each CALIOP scene and is subtracted from the total backscatter. This removes any background backscatter, leaving only the backscatter caused by the presence of clouds or the ash plume. For each CALIOP pixel the cumulative backscatter value is calculated descending through the atmosphere and the cloud top height is considered to be at the altitude at which the atmospheric extinction passes a given threshold. For the purpose of this study, and given the manageable number of scenes considered, the threshold value is calculated individually for each scene and chosen to be the value that best matches the CALIOP image.
Due to the narrow swath of the CALIOP instrument, there are only eight coincidences (119 pixels in total) between the two satellite datasets where the CALIOP track intersects with the volcanic plume seen by IASI. This leads to only a few scenes available for comparison. Shown here are examples from the Eyjafjallajökull eruption in April/May 2010.

Figure 8 shows an overpass of Eyjafjallajökull on 6 May 2010. The co-location for this scene is good (within 1.5 h and 50 km), with the CALIOP track directly crossing the retrieved IASI plume top altitude (circles) and the derived CALIOP plume top altitude (triangles) are overplotted onto the CALIOP backscatter. 

Figure 9 shows the results of comparisons between the retrieved IASI altitude and the derived CALIOP plume height for the Eyjafjallajökull eruption on 6 and 11 May 2010.

5.3.3 Results

The results for an overpass of Eyjafjallajökull on 6 May 2010. The derived CALIOP cloud top heights (triangles) and the retrieved IASI plume top altitude (circles) are overplotted onto the CALIOP backscatter. 

Figure 8. The results for an overpass of Eyjafjallajökull on 6 May 2010. The derived CALIOP cloud top heights (triangles) and the retrieved IASI plume top altitude (circles) are overplotted onto the CALIOP backscatter.

Figure 9. The results of comparisons between the retrieved IASI altitude and the derived CALIOP plume height for the Eyjafjallajökull eruption on 6 and 11 May 2010.

the results shown in this paper to the results obtained using the multiple layers.

Comparisons are not shown for all scenes individually; however, Fig. 10 shows the comparison for all points across all scenes. Some scenes have far fewer co-located pixels but do confirm that there is agreement between the CALIOP and IASI derived altitude range, with the values largely occurring between 2 and 6 km. Despite good correlation in individual scenes, it is very low for all pixels, $r = 0.12$, with RMSE of 2.1 km. Visually, it can be seen that there are cases where the retrieval fails to fully capture the higher-altitude plumes and there is an underestimation of the plume top height (as previously described); however, this is for only two of the scenes, and given the time difference between the satellite overpasses, it is possible that the plume may have been transported vertically through the atmosphere during that time, and therefore small discrepancies are expected. Further, in general, these pixels tend to be optically thick, which may indicate that the IASI retrieval method is assuming a lower altitude and higher AOD in order to fit the measured spectra, whereas in reality the scene has a lower optical depth at higher altitude. This is symptomatic of the optimal estimation method and will be investigated further to reduce its occurrence. It should be noted that in many scenes sections of the plume are above layers of high backscatter, e.g. Fig. 8, which are low altitude meteorological cloud. In these cases the retrieval still performs well, although, as stated, some underestimation in the plume top altitude is observed, caused by the multiple layers.

The results shown follow the criterion established in Sect. 4: carry out the retrieval using the clear covariance matrix; then, if the retrieval fails (or does not pass the quality control), repeat using the cloudy covariance matrix. The robustness of this criterion was confirmed, by comparing the results shown in this paper to the results obtained using purely the cloudy covariance (not shown), with the latter performing worse.

6 Conclusions

A new optimal estimation scheme has been developed for the detection and characterization of volcanic ash plumes using IASI measurements. Pixel-by-pixel estimates are derived for the properties of the volcanic ash: ash optical depth, effective radius, plume top altitude, and effective radiating temperature, with associated uncertainty estimates.

The measurement error covariance matrix is created using difference spectra, which are the residuals between IASI measurements and simulated spectra (calculated using RTTOV with ECMWF operational data). This ensures that all inaccuracies in the radiative transfer modelling of the IASI spectrum, caused by lack of knowledge of the background atmospheric conditions (e.g. atmospheric profiles) or imperfections in the radiative transfer calculation (e.g. spectroscopy), are accounted for within the covariance matrix. Separate covariance matrices have been created using only clear-sky or cloudy scenes, where the latter contains the variance caused by the impact of meteorological cloud. It should be noted that this does not account for errors in the ash optical properties.

A sensitivity study has been carried out using both the clear-sky and cloudy covariance matrices, which showed that the clear covariance consistently produced smaller resultant uncertainty due to the smaller variance it contains. However, this only considers clear-sky synthetic spectra. Therefore, the criterion that is enforced first iterates the retrieval using the clear covariance matrix; then, if the retrieval fails to pass the quality control tests (e.g. convergence), the retrieval is re-run using the cloudy covariance matrix. The uncertainty analysis demonstrates that the uncertainty in AOD, effective radius, and plume top altitude is higher for optically thin plumes, and for AOD and effective radius; this further increases as the plume nears the surface. In contrast to this, the uncertainty on plume top altitude decreases at lower altitudes.

The results of comparisons between the retrieved volcanic ash properties and measurements from other instruments have been shown. The AOD has been show to have good agreement with retrievals carried out using the MODIS instrument on board NASA TERRA. This is especially true at lower AOD (RMSE: 0.15–0.2) with an increase in spread at increasing AOD (RMSE: 0.46). Aircraft campaigns during the Eyjafjallajökull eruption confirm that the retrieved distribution of effective radii from IASI is in line with the aircraft measurements, skewing towards slightly smaller particles due to viewing a larger area of the plume and therefore a slightly different distribution of the ash. Comparing the derived cloud top heights from CALIOP and retrieved IASI plume top heights further illustrates the robustness of the retrieval, with RMSE values consistently less than 2 km.

Figure 10. The results of comparisons between the retrieved IASI altitude and the derived CALIOP plume height for all scenes during the the Eyjafjallajökull eruption. The different colours indicate different scenes.
Underestimation of the plume top altitude in optically thick pixels is observed, which is thought to be caused by the physical thickness of the plume, or the existence of multiple layers within the plume, which are not accounted for in the forward model.

Future work will aim to improve the current limitations within the retrieval and examine further ways to fully capture high plumes and account for the presence of cloud within the IASI scenes through the inclusion of another cloud (or ash) layer within the retrieval process (a two-layer forward model) and an improved selection of channels specifically chosen to minimize the impact caused by clouds.

7 Data availability

The data shown in this paper for the Eyjafjallajökull eruption can be made available on request to the author (lucy.ventress@physics.ox.ac.uk). The IASI ash detection algorithm (IASI NRT, 2016) output is available in near-real time at http://www.nrt-atmos.cems.rl.ac.uk.

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