Parameterization retrieval of trace gas volume mixing ratios from Airborne MAX-DOAS

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Abstract. We present a parameterization retrieval of volume mixing ratios (VMRs) from differential slant column density (dSCD) measurements by Airborne Multi-AXis Differential Optical Absorption Spectroscopy (AMAX-DOAS). The method makes use of the fact that horizontally recorded limb spectra (elevation angle 0°) are strongly sensitive to the atmospheric layer at instrument altitude. These limb spectra are analyzed using reference spectra that largely cancel out column contributions from above and below the instrument, so that the resulting limb dSCDs, i.e., the column integrated concentration with respect to a reference spectrum, are almost exclusively sensitive to the atmospheric layers around instrument altitude. The conversion of limb dSCDs into VMRs is then realized by calculating box air mass factors (Box-AMFs) for a Rayleigh atmosphere and applying a scaling factor constrained by O₄ dSCDs to account for aerosol extinction. An iterative VMR retrieval scheme corrects for trace gas profile shape effects. Benefits of this method are (1) a fast conversion that only requires the computation of Box-AMFs in a Rayleigh atmosphere; (2) neither local aerosol extinction nor the slant column density in the DOAS reference (SCDₜₐₐₐ) needs to be known; and (3) VMRs can be retrieved for every measurement point along a flight track, thus increasing statistics and adding flexibility to capture concentration gradients.

Sensitivity studies are performed for bromine monoxide (BrO), iodine monoxide (IO) and nitrogen dioxide (NO₂), using (1) simulated dSCD data for different trace gas and aerosol profiles and (2) field measurements from the Tropical Ocean iRoposphere Exchange of Reactive halogen species and Oxygenated VOC (TORERO) field experiment. For simulated data in a Rayleigh atmosphere, the agreement between the VMR from the parameterization method (VMRpara) and the true VMR (VMRtrue) is excellent for all trace gases. Offsets, slopes and R² values for the linear fit of VMRpara over VMRtrue are, respectively (0.008 ± 0.001) pptv, 0.988 ± 0.001, 0.987 for BrO; (−0.0066 ± 0.0001) pptv, 1.0021 ± 0.0003, 0.9979 for IO; (−0.17 ± 0.03) pptv, 1.0036 ± 0.0001, 0.9997 for NO₂. The agreement for atmospheres with aerosol shows comparable R² values to the Rayleigh case, but slopes deviate a bit more from one: (0.093 ± 0.002) pptv, 0.933 ± 0.002, 0.907 for BrO; (0.0021 ± 0.0004) pptv, 0.887 ± 0.001, 0.973 for IO; (8.5 ± 0.1) pptv, 0.8302 ± 0.0006, 0.9923 for NO₂. VMRpara from field data are further compared with optimal estimation retrievals (VMROE). Least orthogonal distance fit of the data give the following equations:

BrOpara = (0.1 ± 0.2) pptv + (0.95 ± 0.14) × BrOtrue;
IOpara = (0.01 ± 0.02) pptv + (1.00 ± 0.12) × IOtrue;
NO₂para = (3.9 ± 2.5) pptv + (0.87 ± 0.15) × NO₂true.

Over-all, we conclude that the parameterization retrieval is accurate with an uncertainty of 20 % for IO, 30 % for BrO and NO₂, but not better than 0.05 pptv IO, 0.5 pptv BrO and 10 pptv NO₂. The retrieval is applicable over a wide range of atmospheric conditions and measurement geometries and not limited to the interpretation of vertical profile measurements in the remote troposphere.

1 Introduction

Airborne Multi-AXis Differential Optical Absorption Spectroscopy (AMAX-DOAS) measurements are well suited to probe the vertical distribution of trace gases such as bromine.
monoxide (BrO), iodine monoxide (IO), nitrogen dioxide (NO₂), glyoxal (CHOCHO), formaldehyde (HCHO), nitrous acid (HONO) or the oxygen collision complex O₄ (Melamed et al., 2003; Wang et al., 2005, 2006; Heue et al., 2005, 2011, 2014; Bruns et al., 2006; Dix et al., 2009, 2013; Merlaut et al., 2011; Prados-Roman et al., 2011; Baidar et al., 2013a, b; Oetjen et al., 2013; Baidar et al., 2015; Volkamer et al., 2015; Werner et al., 2016). AMAX-DOAS collects scattered sunlight along multiple lines of sight by changing the viewing direction of the light-collecting telescope to different elevation angles (EAs), here defined as the angle between horizon and line of sight. The selective combination of instrument and solar geometries maximizes sensitivity to different altitude layers in the atmosphere by enhancing the light paths through these layers. Generally MAX-DOAS measurements are most sensitive to absorbers at instrument altitude when using low EAs, while the sensitivity to stratospheric trace gases depends mostly on solar zenith angle (Hönninger et al., 2004). Trace gas differential slant column densities (dSCDs) are the primary product (level 1 data) when analyzing scattered light spectra with the DOAS technique (Platt and Stutz, 2008). DSCDs quantify the integrated concentration along all light paths contributing to the measured spectrum with respect to a reference spectrum, i.e., dSCD = SCD − SCD_ref, where SCD_ref is the slant column contained in the reference spectrum. In order to convert light-path-dependent dSCDs into a light-path-independent quantity, i.e., a vertical column density (VCD, the integrated concentration along a vertical column through the atmosphere) or a vertical concentration density (VCD, the integrated concentration along a vertical column through the atmosphere) or a vertical concentration profile, the light paths contributing to each dSCD measurement need to be known. Photon paths can be simulated by radiative transfer models (RTMs). Since aerosol and clouds can strongly affect light path distributions, a typical method to retrieve VCDs or profile data from MAX-DOAS measurements is a two-step process. First, the aerosol extinction profile is retrieved, e.g., by utilizing information contained in measurements of O₄ (Wagner et al., 2004), which has an atmospheric profile that is well described by local temperature and pressure (Thalman and Volkamer, 2013). Second, trace gas concentrations are retrieved through an inversion technique that applies RTM computed weighting functions for an atmosphere, including the prior retrieved aerosol extinction. This approach is well suited for individual case studies, but it is typically time consuming, computationally intensive and requires vertically resolved SCD measurements as input. The widespread application of MAX-DOAS measurements from ground, ship, aircraft, balloon or satellite platforms and the accumulation of large data sets has led to recent developments that parameterize radiative transfer to interpret DSCD measurements (Sinreich et al., 2010, 2013; Irie et al., 2011; Schreier et al., 2016). Building on Sinreich et al. (2013), we present a parameterization retrieval of volume mixing ratios (VMRs) from AMAX-DOAS trace gas dSCDs. This study is organized as follows: Sect. 2 introduces the general principle of the retrieval, Sect. 3 describes a series of sensitivity studies using simulated data, while Sect. 4 discusses errors, strengths and limitations of the method. The parameterization retrieval is then applied to Tropical Ocean tRoposphere Exchange of Reactive halogen species and Oxygenated VOC (TORERO) field data in Sect. 5. Agreement with select optimal estimation (OE) results is evaluated and TORERO IO and BrO results are discussed. Section 6 summarizes results and concludes on strengths and limitations of the retrieval.

2 Parameterization retrieval

2.1 General principle

The parameterization approach exploits the fact that spectra measured with EA 0° are highly sensitive to instrument altitude. An EA 0° spectrum is analyzed relative to a suitable reference spectrum, e.g., a zenith reference. As a result, trace gas contributions from atmospheric layers above and below the instrument are mostly canceled out and the respective dSCD is representative of a range of altitudes near the instrument altitude. The sensitivity of such an EA 0° dSCD measurement is quantified by box air mass factors (Box-AMFs) that are calculated for a Rayleigh atmosphere. Box-AMFs describe the sensitivity of a measurement to the partial VCD of an atmospheric layer. For optically thin absorbers, such as discussed here, the calculation of Box-AMFs is independent of the trace gas profile. Figure 1 shows dBbox-AMFs (dBbox-AMF = Bbox-AMF = Bbox-AMFref) simulated at 477 nm for an instrument altitude of 5.25 km and a zenith reference from 7.75 km. The Box-AMFs are calculated on a vertical grid with a total number of N layers, where each layer n has a constant grid height (dh) of 0.5 km up to 19 km and 1–2.5 km grid boxes above. The strong enhancement of dBbox-AMFs at instrument altitude indicates the greatly enhanced sensitivity of AMAX-DOAS at instrument altitude. The altitude range with the largest dBbox-AMFs is called the sensitive range, S (grey shading in Fig. 1). It is demarcated by lower and upper boundary layers, nL and nU. Initial sensitivity studies have shown that the parameterization method typically works best when about 90 % of the sum over the dBbox-AMF trace is included in S. Therefore the lower boundary nL is set to 1 km below the instrument layer, ninstr, while nU is set to the altitude layer before the difference between two consecutive dBbox-AMFs is smaller than 10 %, and no more than 3.5 km above ninstr. Due to the distinct shape of the dBbox-AMF (Fig. 1), the placement of the lower boundary is less critical and remains fixed, while the placement of the upper limit is more flexible. The dependency of S on altitude, reference and wavelength is shown in Fig. S1 in the Supplement.

The basis of the parameterization retrieval is to treat each EA 0° dSCD as a measurement of S, i.e., dSCD ≈ dSCD(S), and then retrieve the trace gas concentration for the layer n at instrument altitude, ninstr (red shading in Fig. 1). To account for the effect of aerosol extinction on Box-AMFs in S,
where dBAMF$_n$ is the dBox-AMF value in layer $n$. The initial iteration, $i = 0$, assumes that the trace gas concentration $c_i^0$ is constant inside $S$. Subsequent iterations calculate $f_{TG}^i$ and $c_i^f$ using prior iteration $c_i^f$ values retrieved during aircraft ascent or descent. Concentration values between maximum aircraft altitude and $n_U$ are interpolated using relative profile information from an atmospheric model. Convergence is typically achieved after the third iteration ($i = 2$) (see Fig. S2.).

The factor $f_{O_4}$ accounts for the O$_4$ profile shape effect on the scaling of the dBox-AMFs. It is calculated as

$$f_{O_4} = \frac{\sum_c^N c(O_4)_n \cdot dh \cdot dBAMF_n}{\sum_{nL}^n dh \cdot dBAMF_n},$$

(4)

All Box-AMFs are simulated for the wavelength of the trace gas of interest (see Table 1). The difference in absorption wavelength between the measured O$_4$ and trace gas dSCD is accounted for by $f_{WL}$:

$$f_{WL} = \frac{a_n(\lambda)}{O_4 \text{ dSCD}} + b_n(\lambda) + c_n(\lambda) \cdot O_4 \text{ dSCD},$$

(5)

where $a_n(\lambda)$, $b_n(\lambda)$ and $c_n(\lambda)$ are wavelength-dependent second-order polynomial coefficients for each altitude layer $n$. The polynomial coefficients are derived by first simulating O$_4$ dSCDs for different aerosol extinction profiles at all O$_4$ and trace gas wavelengths, and then applying altitude-dependent fits to O$_4$ dSCDs at each trace gas wavelength plotted over O$_4$ dSCDs at the nearest O$_4$ wavelength. See Sect. 3.1.2 for further details.

The volume mixing ratio at instrument altitude, VMR$_{instr}$, is derived by dividing the final iteration $c_i^f$ derived with Eq. (1) by the air number density of $n_{instr}$. All VMRs in this study are expressed in pptv, i.e., parts per trillion ($1 \times 10^{-12}$) by volume.

Since more than half of the O$_4$ concentration profile is located below 4 km, the suitability of O$_4$ as scaling factor with increasing altitude needs to be assessed. Figure 2 investigates the altitude-dependent sensitivity of O$_4$ measurements. Panel a shows EA 0° SZA measurement for a Rayleigh atmosphere for a solar zenith angle (SZA) range between 0 and 70°. The reference spectrum to create dSCDs has a SZA of 25° and is from 14.75 km altitude, which is the maximum altitude for this study and representative of the range of altitudes covered during the TORERO project. Values above 15 km are included for reference, since some other research aircraft have the capability to access these higher altitudes. The comparatively strong O$_4$ absorption allows the significant detection of O$_4$ dSCDs of up to 20 km at 477 nm and up to 18 km at 360 nm, assuming a detection limit of $2 \times 10^{41}$ molec$^2$ cm$^{-5}$ and $5 \times 10^{41}$ molec$^2$ cm$^{-5}$, respectively, which means that O$_4$ detection is not a limiting factor for the altitude range of this study. Moreover, Fig. 2b shows the fraction of the O$_4$ signal coming from outside the sensitive range $S$, for both
Table 1. RTM settings.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>RTM value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wavelength</td>
<td>350 nm (BrO); 428 nm (IO); 447 nm (NO$_2$); 360 and 477 nm (O$_4$)</td>
</tr>
<tr>
<td>SZA</td>
<td>0, 10, 25, 40, 50, 60, 70°</td>
</tr>
<tr>
<td>SRAA</td>
<td>90°</td>
</tr>
<tr>
<td>EA</td>
<td>0, 10, 90°</td>
</tr>
<tr>
<td>Altitude</td>
<td>SZA 0°: 0.1 km, 0.25–14.75 km in 0.5 km increments</td>
</tr>
<tr>
<td></td>
<td>SZA 10°: 11.25, 12.25, 13.25, 14.25, 14.75 km</td>
</tr>
<tr>
<td></td>
<td>SZA 90°: 0.1, 4.25, 7.75, 11.25, 12.25 km</td>
</tr>
<tr>
<td>Ground albedo</td>
<td>350/360 nm: 0.05, 428–477 nm: 0.08</td>
</tr>
<tr>
<td>g-parameter*</td>
<td>marine: 0.75; urban: 0.69; mixed: 0.72</td>
</tr>
<tr>
<td>SSA*</td>
<td>marine: 0.98; urban: 350/360 nm: 0.92, 428–477 nm: 0.94; mixed: 0.96</td>
</tr>
</tbody>
</table>

* Settings based on Dubovik et al. (2002).

2.2 Correction of dSCD contributions from outside $S$

The accuracy of $c_{\text{inlay}}$ retrieved with Eq. (1) depends on the availability of a reference spectrum to cancel out dSCD contributions from above and below the sensitive range $S$. Ideally each set of EA 0° dSCD measurements has a reference recorded under the same atmospheric conditions. Actual field data might not contain a sufficient amount of suitable references for a variety of reasons. Therefore a dSCD correction term is included, $dSCD^i_c$, to account for contributions from outside $S$ that are not canceled out by the reference. For example strong profile gradients, or a difference in SZA between reference and measurement, can lead to significant EA 0° dBox-AMF values outside $S$ and thus create significant dSCD contributions from outside $S$. Particularly for absorbers with a large stratospheric VCD, a small change in SZA can significantly affect the dSCD value. The additive term $dSCD^i_c$ is separated in a tropospheric and stratospheric contribution term:

$$dSCD^i_c = dSCD^i_{\text{trop}} + dSCD^i_{\text{strat}}.$$  (6)

The tropospheric slant column correction, $dSCD^i_{\text{trop}}$, is defined as

$$dSCD^i_{\text{trop}} = -dh \cdot \sum_{n=0}^{n_{\text{max}}} c^i_n \cdot d\text{BAMF}_n$$

for $i > 0$ and $n \neq n_L \ldots n_U$.  (7)

$dSCD^i_{\text{trop}}$ is calculated from the surface to maximum aircraft altitude (layer $n_{\text{max}}$) for all $n$ below $n_L$ and above $n_U$ using prior iteration $c^i_n$ values retrieved during aircraft ascent or descent. For $i = 0$, $c^0_n$ is set to zero and hence $dSCD^i_{\text{trop}}$ is zero. Note that the distinction between tropospheric and stratospheric contributions is based on aircraft maximum altitude here, not on actual tropopause height.

The stratospheric correction is calculated from layer $n_{\text{max}}$ to $N$, i.e., the top of the atmosphere, and is applied to absorbers with a significant stratospheric VCD – here, BrO and O$_4$. On average only 10% of the dSCD signal originates from outside $S$, which makes the O$_4$ dSCDs very suitable for use as scaling factor. Increasing fractions below 5 km at 360 nm are due to stronger Rayleigh scattering, which decreases the vertical extent of $S$ and the magnitude of the dBox-AMF forward peak. Even though O$_4$ SCDs are not directly used for the parameterization retrieval, the increase of outside contributions to the total O$_4$ SCD with altitude are an indication of the increased error sensitivity of the O$_4$ dSCD towards inaccurate subtraction of outside contributions by the reference spectrum. We conclude that using measured O$_4$ dSCDs as an aerosol scaling factor is limited to altitudes below 15 km. For further discussion on the O$_4$ dSCD error see Sect. 4.
where the subscript “in” refers to layers between and “above” to layers (n_{\text{U}} + 1) to \( N \). AMFs and dAMFs are the sum over Box-AMFs/dBox-AMFs scaled by the trace gas profile. The profile information comes from an atmospheric model.

VCD(t)_{\text{strat}} is derived by dividing the EA 10^\circ dSCD at time \( t_0 \) by dAMF(t_0, EA 10^\circ)_{\text{strat}}. Contributions from layers below \( n_{\text{max}} \) to the EA 10^\circ dSCD are assumed to be canceled out by the reference. VCD(t)_{\text{strat}} at the time of measurement is calculated as EA 10^\circ dSCD(t) + SCD(t_0)_{0^\circ} divided by AMF(t, EA 10^\circ)_{\text{strat}}. Here, SCD and AMF are used instead of dSCD and dAMF to avoid increased uncertainties created by the division of two small numbers. The stratospheric amount contained in the reference, SCD(t_0)_{0^\circ}, can easily be calculated from VCD(t_0)_{\text{strat}}. When reference and measurement are close in time, dSCD_{\text{strat}} approaches \( \Delta dSCD(t) \).

3 Application to synthetic data

In order to define filter criteria for conditions under which the parameterization retrieval is suitable for field data, a series of sensitivity studies were conducted, using synthetic data. The synthetic data set consists of BrO, IO and NO\textsubscript{2} dSCDs simulated for different trace gas and aerosol extinction profiles (Fig. 3). Details on the setup are provided in Sect. 3.1. BrO and NO\textsubscript{2} are both gases for which a significant portion of the total VCD resides in the stratosphere. IO, CHOCHO and HCHO are mostly tropospheric absorbers, for which IO is discussed here as an example. The parameterization retrieval is first tested on trace gas dSCDs simulated for a Rayleigh atmosphere followed by a study on how the VMR retrievals of the same trace gas profiles are affected by different aerosol extinction profiles.

### 3.1 Setup

#### 3.1.1 Trace gas and aerosol profiles

Vertical trace gas profiles of BrO, IO and NO\textsubscript{2} as well as aerosol extinction profiles used to simulate dSCD data are shown in Fig. 3. There are three different profiles for each trace gas, named a, b and c. The a profiles peak strongly in the boundary layer and have a constant mixing ratio throughout the troposphere above. The NO\textsubscript{2} a profile is selected to represent a polluted boundary layer. All b profiles exhibit an elevated layer. The IO b profile is based on TORERO measurements near the coast of Antofagasta, Chile, where an IO layer around 2 km altitude was observed (see also Fig. 7). The NO\textsubscript{2}
b profile overlaps with the aerosol extinction layer of extinction profile 3, simulating an elevated pollution layer. BrO and IO c profiles are smoothed TORERO campaign averages for the tropics based on initial parameterization runs (this work). The NO$_2$ c profile is a case study from TORERO research flight (RF) 12 as published in Volkamer et al. (2015). Tropospheric VCDs from the surface to 18 km for a, b and c profiles are $1.4 \times 10^{13}$, $2.4 \times 10^{13}$ and $1.7 \times 10^{13}$ molec cm$^{-2}$ for BrO, $5.0 \times 10^{12}$, $8.6 \times 10^{12}$ and $3.4 \times 10^{12}$ molec cm$^{-2}$ for IO and $42.5 \times 10^{14}$, $8.0 \times 10^{14}$ and $2.7 \times 10^{14}$ molec cm$^{-2}$ for NO$_2$, respectively. Stratospheric profiles for BrO and NO$_2$ are based on Realtime Air Quality Modeling System (RAQMS) (Pierce et al., 2003, 2007) for the TORERO study area with VCD$_{strat} = 1.1 \times 10^{13}$ and $1.3 \times 10^{15}$ molec cm$^{-2}$ for BrO and NO$_2$ respectively (see Fig. S3 for profile shape). Profiles were created by averaging and smoothing 30 stratospheric profiles, 5 each from RF01, RF04, RF05, RF12, RF14 and RF17, chosen from flight periods with a consistent tropopause between 17 and 18 km. IO profile concentrations are 0 above 18 km. The aerosol extinction profiles vary in shape, absolute values and composition. Profiles 1 through 3 (Fig. 3) are assumed to represent a clean marine (1), a polluted urban (2) and a semi-polluted (3) environment. The latter consists of marine aerosols in the boundary layer and an urban pollution layer aloft. Profile 1 is similar to extinction we found over pristine ocean during the TORERO project. Profiles 2 and 3 are constructed specifically for the sensitivity studies here to investigate the effects of higher aerosol optical depth (AOD) (1) and lofted pollution (2). Details on the representation of aerosol in the RTM are given in the following section and Table 1.

3.1.2 Radiative transfer modeling

All Box-AMFs used in this study are calculated with McAr-tim (Deutschmann et al., 2011), which is a fully spherical Monte Carlo radiative transfer model. Table 1 provides a summary of RTM settings that were used to compute Box-AMFs for the sensitivity studies. The SZA is varied between 0 and 70°, while the solar relative azimuth angle (SRAA) is kept constant at 90°. All model calculations are performed on a 0.5 km vertical grid up to 19 km, which is representative of the vertical resolution of our TORERO AMAX-DOAS measurements. EA 0° measurements are simulated for 0.1 km and from 0.25 to 14.75 km in 0.5 km steps. For zenith spectra, the reference altitude, $h_{ref}$, is varied between 0.1 and 12.25 km (see Table 1). Above 12.5 km, the zenith sky is considered too dark to obtain high-quality spectra. EA 10° reference spectra are simulated for altitudes between 11.25 and 14.75 km (see Table 1). Reference selection is further discussed in Sect. 3.1.3. The model wavelengths for which Box-AMFs are calculated are selected to match the center wavelength of individual trace gas DOAS fitting windows (Volkamer et al., 2015; Wang et al., 2015), i.e., 350 nm for BrO, 428 nm for IO, 447 nm for NO$_2$ and 360 and 477 nm for O$_4$. The model atmosphere is set up to represent conditions over a tropical ocean as found during TORERO. It includes profiles of ozone (VCD = $7.0 \times 10^{18}$ molec cm$^{-2}$/260.2 DU), H$_2$O (VCD = $1.79 \times 10^{23}$ molec cm$^{-2}$), NO$_2$ (VCD = $2.76 \times 10^{16}$ molec cm$^{-2}$) and O$_4$ (VCD = $3.1 \times 10^{15}$ molec cm$^{-2}$). The O$_4$ profile is corrected for oxygen displacement by water vapor, because the very high water mixing ratios found in the tropical marine boundary layer can decrease collocated O$_4$ concentrations by up to 5% (Thalman and Volkamer, 2013; Spinei et al., 2015). Surface temperature, pressure and water mixing ratio are 300.2 K, 1010.5 mbar and 3.1% respectively. Trace gas, temperature and pressure profiles were created by averaging and smoothing 30 individual profiles, 5 each from RF01, RF04, RF05, RF12, RF14 and RF17. Stratospheric ozone and tropospheric NO$_2$ profiles are from RAQMS. For ozone flight periods with a consistent tropopause between 17 and 18 km are chosen, and for NO$_2$ areas with pristine background air. Tropospheric ozone, H$_2$O, temperature and pressure are from aircraft in situ measurements and averaged over the same periods as model profiles. Aerosols are included using extinction profiles (Fig. 3), single scattering albedo (SSA) and the g-parameter as representation for the aerosol phase function (Henyey and Greenstein, 1941). Values for SSA and g-parameter are chosen based on Fig. 1 and Table 1 in Dubovik et al. (2002). To simulate trace gas and O$_4$ SCDs at other wavelengths, aerosol extinction profiles are scaled from 477 nm assuming an Ångström exponent of one. DSCDs are created using references as described below (Sect. 3.1.3). In order to get the wavelength and altitude-dependent fit coefficients that define $f_{sc}$ (Eq. 5), O$_4$ dSCDs simulated for all extinction profiles are separated by altitude layers $n$. For each $n$, respective O$_4$ dSCDs at 447 and 428 nm are each plotted over O$_4$ dSCDs at 477 nm and fitted with a second-order polynomial. The same is done for O$_4$ dSCDs at 350 nm, but plotted over O$_4$ dSCDs at 360 nm. The resulting fit parameters are stored in a lookup table and applied in Eq. (5) during the VMR retrieval to interpolate the measured O$_4$ dSCDs in Eq. (1). The same process is applied to interpolate Rayleigh Box-AMFs from 477 to 447 and 428 nm, and from 360 to 350 nm, in order to save RTM computation time. For example, for a near-real-time application of the parameterization retrieval during a field project, a significant amount of computation time can be saved, when for each research flight Box-AMFs along the flight track are calculated at two O$_4$ wavelengths, instead of at all trace gas wavelengths.

3.1.3 Reference spectra

For our sensitivity studies, BrO and NO$_2$ are analyzed with a zenith reference (EA 90°). Since the sky becomes increasingly dark with altitude, upward-looking EA 10° spectra from aircraft maximum altitude are a light-strong alternative for absorbers without significant stratospheric VCDs. O$_4$ and IO are therefore analyzed with high-altitude EA 10° ref-
ferences. A further advantage of EA 10° references is that in the presence of aerosols EA 10° Box-AMFs from high-altitude spectra resemble EA 0° Box-AMFs outside S more closely than those of zenith references, thus canceling out distributions from outside S more accurately (Volkamer et al., 2015). Altitudes for both zenith and EA 10° references are listed in Table 1. For IO, trace gas and O₄ references are identical. When retrieving BrO and NO₂, O₄ is analyzed with an EA 10° reference from aircraft maximum altitude, here 14.75 km. Trace gas and O₄ references have the same SZA. For a more detailed discussion on suitable references for BrO, IO and NO₂ see Volkamer et al. (2015).

3.2 Sensitivity studies

SCDs were simulated for all trace gas and aerosol extinction profiles shown in Fig. 3 and for settings summarized in Table 1. Parameters of interest that are varied are SZA, ΔSZA, i.e., the SZA difference between EA 0° and reference measurement, and the reference altitude $h_{\text{ref}}$. Trace gas dSCDs were created by permuting through every reference for each combination of trace gas and aerosol profiles, for a total of 2940 different full profile case studies. For the VMR retrieval only dSCDs larger than $1.5 \times 10^{13}$ molec cm$^{-2}$ for BrO, larger than $2 \times 10^{12}$ molec cm$^{-2}$ for IO and larger than $2 \times 10^{14}$ molec cm$^{-2}$ for NO₂ are considered as significant, and smaller dSCDs are filtered. These limits are based on typical fit uncertainties for the University of Colorado (CU) AMAX-DOAS instrument as reported among other trace gases in Volkamer et al. (2015), i.e., $1.3 \times 10^{13}$ molec cm$^{-2}$ for BrO, $2.1 \times 10^{12}$ molec cm$^{-2}$ for IO and $1.5 \times 10^{14}$ molec cm$^{-2}$ for NO₂. For trace gases with stratospheric VCDs, the maximum SZA is limited to 60°, creating a total of 2160 different full profile case studies for BrO and NO₂. IO dSCD data above $h_{\text{ref}}$ are removed for test cases where $h_{\text{ref}}$ is below aircraft maximum altitude. Further filtering is based on the results of the sensitivity studies and discussed in Sect. 3.2.2.

3.2.1 VMR$_{\text{para}}$ in a Rayleigh atmosphere

Figure 4 presents a summary of VMR retrieval results from trace gas dSCDs simulated for a Rayleigh atmosphere for 735 IO and 540 BrO and NO₂ profile case studies and for $i = 2$ (see Fig. S4 for a comparison of $i = 0$ and $i = 2$). Results are displayed separately for each trace gas and profile shape. All retrieved VMR$_{\text{para}}$ are binned by EA 0° instrument altitude (see Table 1). For each altitude, the average and standard deviation of VMR$_{\text{para}}$ is calculated and plotted in the individual left panels of Fig. 4 together with the original trace gas profile as reference. The green shading indicates ±0.5 pptv for BrO, ±0.05 pptv for IO and ±10 pptv for NO₂. To get further information on the distribution of retrieved VMRs, ratios of VMR$_{\text{para}}$ over true VMR, VMR$_{\text{true}}$, are calculated. These ratios are plotted as vertically resolved whiskers in the individual right panels of Fig. 4. Whiskers denote 5, 25, 75 and 95 percentiles. A ratio of 1 means VMR$_{\text{true}}$ is retrieved without error. Grey shaded areas indicate 15 and 30 % error respectively. Dark green dashed lines show the equivalent of ±0.5, 0.05 and 10 pptv for BrO, IO and NO₂, respectively, calculated by adding or subtracting the respective amount from the true profile before division by the true profile. The light green line represents the dark green line multiplied by 0.1. The agreement between retrieved and true VMRs is excellent for all trace gases and profile shapes. Even 5 and 95 percentile whiskers fall within the 30 % error margin or better. These results demonstrate the accuracy of the stratospheric correction for BrO and NO₂. For BrO and NO₂ c profiles the true mixing ratio falls within 0.5 and 10 pptv respectively. The comparison of the 5 and 95 percentiles indicates a slight low bias of the retrieved VMRs for both BrO and NO₂ across all profile shapes. This bias is primarily caused by negative ΔSZAs, i.e., the SZA of the...
reference is higher than the SZA of the measurement. The impact of $\Delta SZA < 0^\circ$ can be seen in Fig. S4, which shows select VMR$_{para}$ data color coded by SZA, $\Delta SZA$ and $h_{ref}$. SZA here and in the following always refers to the SZA of the measurement spectrum, not the reference. For $i = 0$ the general trend in the retrieved VMRs is that the relative deviation from the true profile increases with increasing SZA. For $\Delta SZA < 0$, VMR$_{para}$ values underestimate the true profile. This is similarly true for reference spectra recorded at low altitudes, e.g., 0.1 km for zenith spectra (BrO and NO$_2$) and 11.25 km for EA$^o$ 10 spectra (IO). The iterative corrections applied during the VMR retrieval significantly improve final results, especially for BrO. The retrieval of IO VMRs is very robust and shows no strong sensitivities to variations in SZA, $\Delta SZA$ or $h_{ref}$, regardless of iteration status. The final VMR$_{para}$ results for $i = 2$ are within $\pm 0.5$ pptv for BrO, $\pm 0.05$ pptv for IO and $\pm 10$ pptv for NO$_2$. While the errors created by a changing SZA and low $h_{ref}$ are essentially eliminated by the iterative corrections, a low bias caused by $\Delta SZA < 0$ remains for BrO and NO$_2$. For example, the VMR ratio of the BrO c profile at 11.25 km altitude with $\Delta SZA = -40^\circ$ and $h_{ref} = 0.1$ km is 0.87, while the ratio at the same altitude with $\Delta SZA = 15^\circ$ and $h_{ref} = 0.1$ km is 1.01. Corresponding ratio values for the NO$_2$ b profile are 0.85 and 0.99. For all 540 Rayleigh profile cases, 100% of BrO VMR$_{para}$ data are retrieved within $\pm 0.5$ pptv of the true profile. Where the true profile falls below 0.5 pptv, 100% is retrieved within 0.5 pptv. For NO$_2$ 96.7% of VMR$_{para}$ data are reproduced within $\pm 10$ pptv and 100% of VMRs below 10 pptv are retrieved within the limit. Where VMR$_{para}$ is outside $\pm 10$ pptv of VMR$_{true}$, 85.8% are retrieved within 30% of VMR$_{true}$. For all 735 IO profile cases, 99.4% of VMR$_{para}$ data are retrieved within $\pm 0.05$ pptv. A summary of these results is included in Table 2 below. Based on these results, we define 0.5, 0.05 and 10 pptv for BrO, IO and NO$_2$, respectively, as (1) suitable detection limits and (2) in combination with a 20% (IO) and 30% (BrO) error suitable error bounds for the parameterization method in a Rayleigh atmosphere.

### 3.2.2 VMR$_{para}$ in aerosol atmospheres

The presence of aerosol in the atmosphere changes Box-AMFs; this is accounted for in the parameterization retrieval by using a measured O$_4$ dSCD in Eq. (1) to scale Rayleigh modeled Box-AMFs. In comparison to results from a Rayleigh atmosphere, the quality of retrieved VMRs in atmospheres with aerosol shows a stronger and more complex dependency on SZA, $\Delta SZA$ and $h_{ref}$. Therefore Fig. 5 presents results for select case studies to highlight these specific dependencies. Summary figures for individual extinction profiles in the style of Fig. 4 are provided in the Supplement (Figs. S5–S7) and discussed in Sect. 4.3. Figure 5 shows VMR$_{para}$ plotted over VMR$_{true}$ for select SZA, $\Delta SZA$ and $h_{ref}$. BrO and IO VMR$_{para}$ are averaged over all trace gas and aerosol profiles. NO$_2$ results are averaged over NO$_2$ b and c profiles (Fig. 3) and all aerosol profiles. Averages of the NO$_2$ a profile are shown in Fig. S8. A total of eight case studies are displayed in panels a through h. Panel columns alternate between low and high SZA (25 and 60$^\circ$). Rows highlight the dependency on $\Delta SZA$ for $\Delta SZA = 0$, 35 and $-15^\circ$, in combination with a variation of $h_{ref}$. Panels a, b, e and f show results with $h_{ref} = 4.25$ km for BrO and NO$_2$ and $h_{ref} = 14.75$ km for IO, which are considered to be optimal references for our case studies. Panels c and d display the effect of using a zenith reference from 0.1 km, while panels g and h show results for a high zenith reference. For a direct comparison, IO data in panels c, d, g and h are also analyzed with zenith references. VMR$_{para}$ data for each panel summarize over nine profile cases for BrO and IO and over six cases for NO$_2$. Whisker plots show 5, 25, 75 and 95 percentiles for binned VMR data. VMRs for BrO are binned in 0.5 pptv intervals and for IO in 0.25 pptv intervals.

### Table 2. VMR retrieval results for synthetic data.

<table>
<thead>
<tr>
<th>Trace gas</th>
<th>Atmosphere</th>
<th>Mean</th>
<th>Standard deviation</th>
<th>Within error$^a$ (%)</th>
<th>Within DL$^b$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>BrO</td>
<td>Rayleigh</td>
<td>0.99</td>
<td>0.06</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>BrO</td>
<td>Aerosol 1</td>
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<td>0.11</td>
<td>99.9</td>
<td>99.9</td>
</tr>
<tr>
<td>BrO</td>
<td>Aerosol 2</td>
<td>1.01</td>
<td>0.14</td>
<td>99.3</td>
<td>97.8</td>
</tr>
<tr>
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<td>Aerosol 3</td>
<td>1.04</td>
<td>0.15</td>
<td>99.7</td>
<td>96.6</td>
</tr>
<tr>
<td>IO</td>
<td>Rayleigh</td>
<td>0.97</td>
<td>0.05</td>
<td>100</td>
<td>99.4</td>
</tr>
<tr>
<td>IO</td>
<td>Aerosol 1</td>
<td>0.92</td>
<td>0.07</td>
<td>98.8</td>
<td>90.8</td>
</tr>
<tr>
<td>IO</td>
<td>Aerosol 2</td>
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<td>0.09</td>
<td>92.8</td>
<td>83.8</td>
</tr>
<tr>
<td>IO</td>
<td>Aerosol 3</td>
<td>0.90</td>
<td>0.13</td>
<td>91.9</td>
<td>85.0</td>
</tr>
<tr>
<td>NO$_2$</td>
<td>Rayleigh</td>
<td>0.99</td>
<td>0.07</td>
<td>99.5</td>
<td>96.7</td>
</tr>
<tr>
<td>NO$_2$</td>
<td>Aerosol 1</td>
<td>1.00</td>
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<tr>
<td>NO$_2$</td>
<td>Aerosol 2</td>
<td>1.00</td>
<td>0.14</td>
<td>94.9</td>
<td>85.1</td>
</tr>
<tr>
<td>NO$_2$</td>
<td>Aerosol 3</td>
<td>1.02</td>
<td>0.14</td>
<td>95.8</td>
<td>78.7</td>
</tr>
</tbody>
</table>

$^a$ ±0.5 pptv or 30% for BrO, ±0.05 pptv or 20% for IO, ±10 pptv or 30% for NO$_2$. $^b$ ±0.5 pptv for BrO, ±0.05 pptv for IO, ±10 pptv for NO$_2$.  

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Figure 5. VMR$_{para}$ over VMR$_{true}$ for BrO (top), IO (middle) and NO$_2$ (bottom) averaged over all BrO and IO trace gas profiles, over NO$_2$ b and c profiles and over all aerosol profiles for select SZA, $\Delta$SZA and $h_{ref}$. The panel columns alternate between low (SZA = 25°) and high (SZA = 60°) SZA. The whisker plots show the median and 5, 25, 75 and 95 percentiles for binned VMR$_{para}$ data. Grey shaded areas indicate 15 and 30 % error. Linear fits and fit parameter (s: slope; o: offset) are included in each panel.
are defined as follows: 20 pptv intervals from 0–80 pptv, then 80–150, 150–400 and 400–1300 pptv. Linear fits to VMR<sub>para</sub> and respective fit parameters, “s” for slope and “o” for offset, are included in each panel. Grey shadings indicate 15 and 30% error respectively.

**Effect of SZA**

VMR retrievals for BrO and NO<sub>2</sub> show a stronger dependency on SZA than those of IO, which can be expected for trace gases with a significant stratospheric VCD. For SZA = 25° and the optimal <i>h<sub>ref</sub></i>, i.e., panels a and e, BrO and NO<sub>2</sub> correlation slopes are on average 0.95 ± 0.01 and 0.905 ± 0.015. Offsets are all below the respective detection limits of 0.5 pptv for BrO and 10 pptv for NO<sub>2</sub> and <i>R<sup>2</sup></i> values are 0.96 (a)/0.97 (e) for BrO and 0.94 for a and e for NO<sub>2</sub>. Results for SZA = 25° and <i>h<sub>ref</sub></i> = 12.25 km (panel g) are comparable for both BrO and NO<sub>2</sub>. Higher SZA increase the stratospheric contribution to the measured dSCDs, which creates a stronger sensitivity to errors in the stratospheric correction. BrO and NO<sub>2</sub> VMR<sub>para</sub> for SZA = 60° with <i>h<sub>ref</sub></i> = 4.25 km and 12.25 km (panels b, f and h) show somewhat lower correlation slopes that are on average 0.89 ± 0.02 for BrO and 0.87 ± 0.02 for NO<sub>2</sub>, but offsets remain below respective detection limits and average <i>R<sup>2</sup></i> values are still high with 0.96 ± 0.01 for BrO and 0.93 ± 0.01 for NO<sub>2</sub>. When looking at the NO<sub>2</sub> a profile only (Fig. S8), then the linear fits are strongly driven by the very high boundary layer VMRs, which is why the NO<sub>2</sub> data set is separated by profile shape here. For the NO<sub>2</sub> a profile the SZA dependence is much more pronounced. For optimal and high references, correlation slopes are around 0.91 for SZA = 25° and around 0.81 for SZA = 60°. In contrast, when using a high-altitude reference spectrum for IO, panels a, b, e through h, correlation slopes are within ±2 percentage points and corresponding offsets are 0.003–0.029 pptv, which is well below the 0.05 pptv detection limit. <i>R<sup>2</sup></i> values are between 0.970 and 0.990.

**Effect of Δ SZA and <i>h<sub>ref</sub></i>**

The impact of ΔSZA and <i>h<sub>ref</sub></i> depends on the combination of both quantities. When using either the optimal or high reference altitude, i.e., panels a, b, e through h, the VMR results for all trace gases are dominated by the SZA effect, as discussed above. Varying ΔSZA between 0, 35 and −15° for a constant SZA, i.e., comparing panels a, e, g and panels b, f, h, leads to differences in correlation slopes that are within ±0.02. Interestingly, a ΔSZA of zero does not always provide the best result because a larger difference in SZA between reference and measurements can actually increase the accuracy of the correction term <i>f<sub>c</sub></i> (Eq. 1). Overall, the combination of ΔSZA = −15 or 35° with a zenith reference from the boundary layer (0.1 km altitude) yields the largest deviations of VMR<sub>para</sub> from VMR<sub>true</sub> for all trace gases. For example, in panel c, the correlation slope drops to 0.89 with <i>R<sup>2</sup></i> = 0.84 for BrO, the slope is 0.845 with <i>R<sup>2</sup></i> = 0.981 for IO and the slope is 0.84 with <i>R<sup>2</sup></i> = 0.92 for NO<sub>2</sub>. The NO<sub>2</sub> a profile shows comparable behavior in panel d, with a slope of 0.77 (Fig. S8). Overall the observed trends are significantly reflected in correlation slopes and <i>R<sup>2</sup></i> values, while offsets are typically very small and well below 50% of the individual trace gas detection limit. Slopes for optimal and high reference spectra indicate that on average VMR<sub>para</sub> are retrieved within 10 to 15% of VMR<sub>true</sub> with tight correlations, i.e., <i>R<sup>2</sup></i> values of 0.92 and better. Based on the combined effect of low <i>h<sub>ref</sub></i> and ΔSZA < 0° an additional filter for the parameterization retrieval is introduced: VMR retrieval of trace gases with stratospheric VCDs are limited to ΔSZA > −25° for <i>h<sub>ref</sub></i> < 2 km. Following the error discussion, results of the full set of sensitivity studies are discussed in Sect. 4.3.

### 4 Error analysis and discussion

#### 4.1 Retrieval error

The underlying assumption of Eq. (1) is that dSCD<sub>4</sub> ≈ dSCD<sub>i</sub>(S), i.e., that the EA 0° dSCD measurement quantifies the trace gas slant column in S (see Sect. 2.1 and Fig. 1). How well this assumption holds true depends on the choice of reference spectrum and the accuracy of the iterative correction term dSCD<sub>c</sub> introduced in Eqs. (6) through (9). The same assumption underlies the measured O<sub>4</sub> dSCDs. Further error sources are insufficient correction of the O<sub>4</sub> and trace gas profile shapes based on Eqs. (3) and (4), and errors caused by the wavelength interpolation of measured O<sub>4</sub> dSCDs based on Eq. (5). The synthetic data set allows the quantification of individual error sources and the overall error. The following error terms are being analyzed here: the error of dSCD<sub>4</sub> and the errors of <i>f<sub>c</sub></i>·<i>f<sub>WL</sub></i>·<i>f<sub>4</sub></i> and <i>f<sub>WL</sub></i>. The magnitude of each error is defined as the ratio of calculated value over true value, which returns 1 when the error is 0. The dSCD<sub>c</sub> error ratio, ΔdSCD<sub>c</sub>, is defined as dSCD<sub>c</sub> divided by dSCD(S). For the <i>f<sub>4</sub></i>·<i>f<sub>WL</sub></i> error ratio, Δ<i>f<sub>4</sub></i>·<i>f<sub>WL</sub></i>, the value of <i>f<sub>c</sub></i> calculated with Eq. (3) is divided by the true <i>f<sub>4</sub></i>·<i>f<sub>WL</sub></i>, i.e., using Eq. (3) and replacing <i>c<sub>i</sub></i> with the true trace gas concentration. The error is calculated with the true trace gas concentration. The <i>f<sub>4</sub></i>·<i>f<sub>WL</sub></i> error ratio, Δ<i>f<sub>4</sub></i>·<i>f<sub>WL</sub></i>, quantifies the ratio of wavelength shifted O<sub>4</sub> dSCDs using Eq. (5) over O<sub>4</sub> dSCDs directly simulated at the respective trace gas wavelength. Note that these error ratios are not random errors, but express a systematic deviation from the true value, which can be calculated for each retrieved VMR data point.
The total error ratio, $\Delta_{\text{total}}$, is defined as the deviation of the calculated trace gas concentration from the true trace gas concentration and is thus identical to $\text{VMR}_{\text{para}}$ over $\text{VMR}_{\text{true}}$. It can be directly calculated from the above introduced error ratios using Eq. (1) as follows:

$$\frac{\text{VMR}_{\text{para}}}{\text{VMR}_{\text{true}}} = \Delta_{\text{total}} = \Delta d\text{SCD}_c^i = \frac{\Delta f_{\text{OA}}}{\Delta f_{\text{TG}}^i \cdot \Delta f_{\text{WL}}}.$$ (11)

Note that this notation is chosen because it explicitly accounts for the fact that individual component errors can compensate each other. All error calculations are performed for $i = 2$. For Rayleigh cases both $\Delta f_{\text{OA}}$ and $\Delta f_{\text{WL}}$ are 1.

Figure 6 shows examples of error ratios plotted over altitude and separated by trace gas and aerosol extinction profiles with $\text{SZA} = 25^\circ$, $\Delta \text{SZA} = 25^\circ$ and $h_{\text{ref}} = 4.25$ km for BrO and NO$_2$ and $h_{\text{ref}} = 14.75$ km for IO. Results are shown for BrO c, IO b and NO$_2$ b profiles. Error ratios for all trace gas profiles are included in the Supplement (Figs. S9–S11). In Figs. 6 and S9–S11, $\Delta f_{\text{TG}}^i$ and $\Delta f_{\text{WL}}$ are plotted inverse in accordance with the fact that they enter the denominator in Eq. (11).

### 4.1.1 $\Delta d\text{SCD}_c^i$

Error ratios from $d\text{SCD}_c^i$ are the dominating error source in a Rayleigh atmosphere and remain a comparatively large error source for atmospheres with aerosols for all trace gases. The magnitude of $\Delta d\text{SCD}_c^i$ is a direct reflection of how well the assumption $d\text{SCD} \approx d\text{SCD}(S)$ holds true. At the selected solar and measurement geometry conditions, $d\text{SCD}_{\text{top}}$ and $d\text{SCD}_{\text{strat}}$ are comparable for both the BrO c profile and the NO$_2$ b profile, with $\sim 1 \times 10^{12}$ molec cm$^{-2}$ for BrO and $\sim 2 \times 10^{14}$ molec cm$^{-2}$ for NO$_2$, which means that the combined tropospheric and stratospheric $d\text{SCD}_c^i$ correction is not dominated by either part of the profile. Stronger deviations are correlated with the absolute trace gas concentration and higher aerosol extinction. For example, for the BrO c profile in the boundary layer, $\Delta d\text{SCD}_c^i$ ranges between 1.5 and 2.7. Here the true profile is < 0.25 pppt, which means that the signal from inside $S$ contributing to the EA $0^\circ$ dSCD measurements is very small. The dashed lines in Fig. 6 show the equivalent of ±0.5 pppt BrO or the scaled equivalent of ±0.05 pppt as reference. $\Delta_{\text{total}}$ for all cases is well below the detection limit of ±0.5 pppt. However, the steep increase in deviations for all error ratios for the BrO c profile below 4 km indicates that the accuracy of VMR$_{\text{para}}$ declines with decreasing dSCDs and that using a detection limit is justified. A strong $\Delta d\text{SCD}_c^i$ deviation from 1 caused by the elevated aerosol layer of aerosol 3 (Fig. 3) is seen for IO and BrO. Here dSCDs are overcorrected, but this error is partially compensated by too-low $f_{\text{OA}}$ values. Interestingly, $\Delta d\text{SCD}_c^i$ is smaller for the NO$_2$ b profile, where the NO$_2$ profile itself has an elevated layer (Fig. 3).

### 4.1.2 $\Delta f_{\text{TG}}^i$

$f_{\text{TG}}^i$ corrects for trace gas gradients within $S$. Hence deviations from one of $\Delta f_{\text{TG}}^i$ are directly related to the trace gas profile shape. In a Rayleigh and sub-Rayleigh atmosphere (see Fig. 3) $\Delta f_{\text{TG}}^i$ is on average around ±2 % and deviates only significantly from 1 where the VMR$_{\text{true}}$ profile has strong concentration gradients, e.g., around the IO layer between 2 and 3 km in the IO b profile, around 7 km for the NO$_2$ b profile, or around 2 km for all trace gas profiles (Figs. S9–S11). The magnitude of the deviation depends on the aerosol extinction. For example, the peak in $\Delta f_{\text{TG}}^i$ at 1.75 km in the IO b profile changes from 1.12 to 1.27 between aerosol 1 and 2, where both extinction profiles have the same shape, but where aerosol 2 has a higher extinction (0.11 vs. 0.02 km$^{-1}$ at 1.75 km altitude). This is similarly true for the NO$_2$ a profile (Fig. S11) at 0.1 km, where $\Delta f_{\text{TG}}^i$ increases from 1.24 to 1.44 between aerosol 1 and 2 (extinctions at 0.1 km are 0.188 vs. 0.037 km$^{-1}$). The overlap of trace gas...
and aerosol extinction gradients as well as higher absolute extinction increases Δf_{1G} deviations from 1, which is typically the case for trace gas and aerosol profiles that represent polluted environments (Sect. 3.1).

4.1.3 Δf_{O4}

The f_{O4} error ratio generally follows the shape and magnitude of the extinction profile as can be expected. For NO2 at 447 nm and IO at 428 nm, f_{O4} tends to overestimate the extinction in the boundary layer (Δf_{O4} > 1) and slightly underestimate the extinction in the free troposphere (Δf_{O4} < 1), where the aerosol extinction is sub-Rayleigh. For BrO, the effect is reversed in the boundary layer and not significant in the troposphere. This result is caused by the differences in the wavelength dependency of Rayleigh and aerosol extinction. Box-AMFs scale with light path length. In the presence of aerosol, the total extinction is determined by Rayleigh and aerosol extinction. Since Rayleigh extinction scales with λ−4 and the aerosol extinction in our sensitivity study scales with λ−1, the (strong) aerosol extinction in the boundary layer at 447 and 428 nm has a comparatively stronger effect at wavelengths above 400 nm than at 350 nm where BrO is measured. The tendency to underestimate extinction in the troposphere above 400 nm is caused by multiple scattering. While the presence of aerosol typically decreases the light path length at instrument altitude, and hence the Box-AMFs within S, increased scattering in aerosol layers below or above instrument altitude can lead to increased contributions from outside S to the measured O4 dSCD. Thus the measured O4 dSCD leads to the underestimation of the real extinction. This effect is amplified for the aerosol layer around 7 km of aerosol profile 3, since enhanced photon backscatter from the boundary layer and the elevated aerosol layer increases the outside contributions to the O4 dSCD measurements inside the layer further, which leads to Δf_{O4} values as low as 0.59 at 447 nm (NO2), 0.58 at 428 nm (IO) and 0.75 at 350 nm (BrO). Interestingly, ΔdSCD_c inside the elevated aerosol layer is overestimated at all wavelengths, with a compensating effect on Δtotal.

4.1.4 Δf_{WL}

The error created by the wavelength interpolation of measured O4 dSCDs is comparatively small. It increases with larger wavelength shifts, e.g., for IO, where O4 dSCDs are shifted from 477 to 428 nm. The f_{WL} error ratio shows no significant altitude dependence and is typically smaller than 5%. The largest Δf_{WL} deviation from 1 is found at 7.25 km altitude for IO and aerosol 3, inside the elevated aerosol layer, with Δf_{WL} = 0.86. This larger deviation is caused by defining the polynomial coefficients used in Eq. (5) as average over all extinction profiles. The reduction of EA 0° O4 dSCDs at different wavelengths is not a linear function of extinction, and interpolation parameters at the altitude of the elevated aerosol layer are biased low by averaging O4 dSCDs from aerosol profile 3 with O4 dSCDs simulated for the sub-Rayleigh extinction of aerosols 1 and 2 at the same altitude. If the polynomial coefficients were generated using only aerosol profile 3, the same Δf_{WL} would increases to 0.92. Notably, the elevated pollution layer is a unique case, and affects only a small number of IO and NO2 VMR_{para} data within a 1.5 km altitude range (see also discussion in Sect. 4.3.1).

4.2 Other error sources

Other errors affecting the accuracy of VMR_{para} are RTM errors and uncertainties in the atmospheric model profiles used to interpolate retrieved trace gas profiles above aircraft maximum altitude. The RTM error encompasses the statistical error of simulating individual photon paths used to calculate the Box-AMFs and the error created by wavelength shifting Box-AMFs (see Sect. 3.1.2). McArtim is initialized with 10^7 photons, which reduces the statistical error to below 0.5% (see also Spinei et al., 2015). Table S1 in the Supplement gives fit coefficients of linear fits to shifted Box-AMF data over original data. Slopes are 0.999 with a 1–2 x 10^−4 error and offsets are ≤ 0.003. Atmospheric model profiles are used to interpolate trace gas profiles above aircraft maximum altitude and calculate stratospheric AMFs. Here, only the relative profile shape is important, since absolute VCD values are canceled out during the AMF calculation. Stratospheric profile shapes of BrO and NO2 are well constrained by models; therefore the error based on profile shape is assumed to be very small and accounted for by the error bounds.

4.3 Summary and overall error

The sensitivity studies in a Rayleigh atmosphere have shown that the parameterization retrieval works very well across a wide range of measurement geometries. VMR retrievals in aerosol atmospheres are more sensitive to SZA and choice of reference spectrum. In Figs. S5–S7 VMR_{para} results for aerosol atmospheres are displayed using the style introduced in Fig. 4; i.e., left panels show mean and standard deviation of VMR_{para} over VMR_{true}. Note that in contrast to Fig. 5 the additional ΔSZA filter is applied here, where for BrO and NO2 the VMR retrieval is limited to ΔSZA > −25° when h_{ref} < 2 km. Compared to a Rayleigh atmosphere the VMR_{para} distribution around the mean has a larger spread. Where the aerosol extinction is sub-Rayleigh (see Fig. 3), the mean stays close to 1 for BrO and NO2. The effect of SZA, ΔSZA and h_{ref} discussed above is captured in the whisker percentiles. For IO the mean tends to deviate from 1 between 2 and 10 km, which is the effect of ΔdSCD_c that is intensified by Δf_{WL} and Δf_{O4} for atmospheres with aerosol as shown in Fig. 6. However, most VMR_{para} data are still retrieved within error bounds. Table 2 summarizes the
mean and 1σ standard deviation of the ratio VMR\textsubscript{para} over VMR\textsubscript{true}, for each trace gas separated by atmospheres. The column “within error” states the fraction of VMR\textsubscript{para} that is retrieved either within the VMR detection limit or within 30 % for BrO and NO\textsubscript{2} and 20 % for IO. The distinction in percentage is based on the stronger sensitivity to SZA, ΔSZA and \(h_{\text{ref}}\) for trace gases with stratospheric VCD. After filtering all VMR\textsubscript{para} data are retrieved on average within 10 % of the error bounds or better.

**Field data**

When applying the parameterization retrieval to dSCD data from the TORERO measurements, dSCDs have associated measurement errors. To test the effect of dSCD errors, VMRs for all trace gas and aerosol profiles were retrieved, adding or subtracting 1.5 \(\times\) 10\(^{13}\) molec cm\(^{-2}\) for BrO, 2 \(\times\) 10\(^{12}\) molec cm\(^{-2}\) for IO and 2 \(\times\) 10\(^{14}\) molec cm\(^{-2}\) for NO\textsubscript{2}. The impact on VMR\textsubscript{para} was assessed by adding the error caused by the measurement uncertainty and the parameterization error in quadrature. On average 92.9 % of resulting VMR\textsubscript{para} data are still retrieved within the above defined error bounds. The fit errors for O\textsubscript{4} dSCDs are typically well below 5 %, with absolute values < 5 \(\times\) 10\(^{11}\) molec\(^2\) cm\(^{-5}\) at 477 m and < 1 \(\times\) 10\(^{12}\) molec\(^2\) cm\(^{-5}\) at 360 nm, and are accounted for by the error bounds. To avoid uncertainties created by fit errors, measured O\textsubscript{4} dSCDs are set equal to Rayleigh modeled dSCDs when their absolute difference is smaller than 5 \(\times\) 10\(^{11}\) molec\(^2\) cm\(^{-5}\) at 477 m and smaller than 1 \(\times\) 10\(^{12}\) molec\(^2\) cm\(^{-5}\) at 360 nm. The uncertainty in determining O\textsubscript{4} SCD\textsubscript{ref} for the absolute scaling of measured O\textsubscript{4} dSCDs is essentially canceled out by using dSCDs and considered negligible.

We conclude that 30 % uncertainty for gases with stratospheric VCD contributions, and 20 % for tropospheric absorbers, but no better than 0.5 pptv BrO, 10 pptv NO\textsubscript{2} and 0.05 pptv IO are suitable error bounds for the parameterization retrieval across different trace gas and aerosol profiles. Errors and sensitivities that arise from strongly changing trace gas VCDs and atmospheric conditions when flying at level altitude will be discussed elsewhere.

**4.3.1 Outliers**

Some VMR\textsubscript{para} data retrieved outside error bounds show significant and systematic deviations from VMR\textsubscript{true}. Examples of such outliers in Fig. 5 are the VMR\textsubscript{para} points that deviate by about 0.6 pptv from VMR\textsubscript{true} for BrO in panel b, deviations of 0.12 pptv from a true VMR of 0.3 pptv for IO in panel b and deviations of around 50 pptv for true values around 100 pptv for NO\textsubscript{2} across all panels. These outliers are not captured by data filtering. This is for example the case for the IO b profile and aerosol profile 1 (Fig. S5), for BrO and NO\textsubscript{2} a profiles and aerosol 2 (Fig. S6) or for IO and NO\textsubscript{2} b profiles and aerosol profile 3 (Fig. S7). When looking at the trace gas profile shapes of the individual left panels in Figs. S5–S7, it becomes apparent that strong gradients in the trace gas profile can shift the retrieved medians significantly away from 1, with partial or full whiskers exceeding the error bounds. In a Rayleigh atmosphere, similar outliers are seen for \(i = 0\), but the iterative corrections bring final VMR\textsubscript{para} data well within error bounds (Sect. 3.2.1 and Fig. S4). In the presence of aerosols the iterative corrections fail when trace gas and aerosol extinction gradients overlap or where extinction is high, like in the lofted pollution layer of aerosol profile 3. These are highly localized effects, but need to be kept in mind when using the parameterization retrieval in areas with strong trace gas and extinction gradients. Under those conditions, OE retrievals are preferred.

**4.3.2 Impact of SCD\textsubscript{ref}**

The selection of a suitable reference spectrum is crucial to best fulfilling the approximation \(\text{dSCD} \approx \text{SCD}(S)\), which is applicable for both trace gas and O\textsubscript{4} dSCDs. Case study results from Figs. 5 and S8, panels c and d, indicate that the VMR retrieval quality decreases and exhibits a low bias when using a boundary layer zenith reference compared to reference spectra from higher altitudes. This observation is a direct result of SCD\textsubscript{ref} being maximized for a boundary layer zenith spectrum and thus decreasing EA 0° dSCDs. Measured EA 0° dSCDs are further decreased for \(\Delta SZA < 0°\), where the comparatively higher SZA of the reference spectrum increases SCD\textsubscript{ref} even more. For example, for SZA = 25°, \(\Delta SZA = -15°\) and \(h_{\text{ref}} = 0.1\) km (Figs. 5c and S8c), SCD\textsubscript{ref} values averaged over aerosol profiles 1–3 are \(3.8 \times 10^{13}\) molec cm\(^{-2}\) for the BrO a profile, \(7.6 \times 10^{15}\) molec cm\(^{-2}\) for the NO\textsubscript{2} a profile and \(7.2 \times 10^{12}\) molec cm\(^{-2}\) for the IO a profile, compared to \(3.2 \times 10^{13}\), \(6.4 \times 10^{15}\) and \(6.1 \times 10^{12}\) molec cm\(^{-2}\) for SZA = 60°, \(\Delta SZA = 35°\) and \(h_{\text{ref}} = 0.1\) km (Figs. 5d and S8d) for BrO, NO\textsubscript{2} and IO respectively. For the optimized conditions, e.g., for SZA = 25°, \(\Delta SZA = 0°\) and \(h_{\text{ref}} = 4.25\) km (BrO, NO\textsubscript{2}) or 14.75 km (IO) (Fig. 5a), SCD\textsubscript{ref} values are \(2.5 \times 10^{13}\), \(3.4 \times 10^{15}\) and \(3.9 \times 10^{12}\) molec cm\(^{-2}\) for BrO, NO\textsubscript{2} and IO respectively. For VMR\textsubscript{para} data that are not retrieved within error bounds, the ratio of EA 0° dSCDs over SCD\textsubscript{ref} is typically smaller 2. These findings underline the importance of reference selection and minimizing SCD\textsubscript{ref}, as, e.g., pointed out by Volkamer et al. (2015) and Coburn et al. (2016), Volkamer et al. (2015) compared ship-based and airborne MAX-DOAS during TORERO, in a case study where the trace gas profile above the ship was characterized by the aircraft. They found best agreement only when SCD\textsubscript{ref} was accounted for in the ship MAX-DOAS retrievals and showed that the widely accepted assumption of SCD\textsubscript{ref} = 0 can lead to bias of up to a factor of 2 for partial VCDs as retrieved from the ship. Maximizing knowledge about SCD\textsubscript{ref} can also be actively exploited to extend the information content in ground-based
MAX-DOAS retrievals of free tropospheric BrO (Coburn et al., 2016).

Finding a suitable reference for O₄ measurements is less straightforward due to the multiple scattering effects described in Sect. 4.1. In fact, using a high-altitude zenith spectrum that typically minimizes SCD_ref leads here to a much stronger underestimation of extinction in the troposphere up to the point where extinction appears to be lower than that of a pure Rayleigh atmosphere. The key to a suitable O₄ reference is finding a reference for which Box-AMFs outside S are most similar to Box-AMFs outside S of the EA 0° spectrum, without minimizing the EA 0° dSCD too strongly. Based on our findings, EA 10° spectra from aircraft maximum altitude are a good match for these criteria, consistent with our earlier recommendation (Volkamer et al., 2015).

4.3.3 Optimized observing strategy parameterization retrieval

As discussed above, minimizing SCD_ref is the best strategy to minimize VMR_para errors. Aircraft measurements allow the recording of reference spectra at different geometries and altitudes, which renders MAX-DOAS particularly suitable for the parameterization retrieval. For unknown trace gas and extinction profile shapes, it is advisable to record several references from different altitude and geometries to not limit the ability to actively minimize SCD_ref.

Data filters that work well for our sensitivity studies are (1) EA 0° dSCD limits of 1.5 × 10⁻¹³ molec cm⁻² for BrO, 2 × 10⁻¹³ molec cm⁻² for IO and 2 × 10⁻¹⁴ molec cm⁻² for NO₂; (2) SZA limit of 60° for stratospheric absorbers; and (3) ΔSZA limit of -25° for h_ref < 2 km. Particularly for stratospheric absorbers, VMR_para are on average retrieved more accurately for ΔSZA ≥ 6°. For a changing SZA and/or changing VCD_strat, the stratospheric correction benefits from continuous VCD characterization by EA 10° measurements.

The interpolation parameter for O₄ dSCDs used in Eq. (5) need to be created for local conditions. In cases of strongly varying extinctions, interpolation might need to be replaced with a lookup table. For strong gradients in trace gas and/or aerosol extinction, OE retrieval is preferred.

5 Application to TORERO field data

During the TORERO field campaign BrO, IO, NO₂, CHO-CHO, HCHO and O₄ were measured with the CU MAX-DOAS instrument aboard the NSF/NCAR GV aircraft over the tropical Eastern Pacific Ocean. The TORERO field experiment took place in January/February, 2012. Seventeen research flights were conducted over the tropical and subtropical Pacific, based out of Antofagasta, Chile, and San Jose, Costa Rica. Further information on the campaign can be found in Volkamer et al. (2015). In this section, the parameterization retrieval is applied to TORERO field data. First, select VMR_para profiles are compared with existing BrO, IO and NO₂ vertical profiles retrieved by OE inversion, followed by a discussion of retrieved BrO and IO VMRs for the whole campaign.

5.1 AMAX-DOAS measurements and data analysis

The CU AMAX-DOAS instrument is described in detail elsewhere (Baidar et al., 2013b; Dix et al., 2013; Volkamer et al., 2015). Briefly, the instrument consists of two synchronized spectrograph–detector units (Acton SP2150/PIXIS400B CCD) that simultaneously observed the spectral ranges from 330 to 470 nm (0.7 nm full width half maximum (FWHM) optical resolution) to measure BrO, IO, NO₂ and O₄ at 360 nm and from 440 to 700 nm (1.2 nm FWHM optical resolution) to observe O₄ at 477 nm. Telescopes to access forward-, zenith- and nadir-viewing geometries are housed in a heated, wing-mounted pylon. The limb scanning telescope has a vertical dispersion of 0.17° and is actively angle stabilized to better 0.2° accuracy in real time. Most limb spectra were recorded with a time resolution of 30 s, which translates to a vertical resolution of 0.5 km or better for most ascents and descents of the aircraft. BrO, IO, NO₂ and O₄ dSCDs were derived from scattered sunlight spectra using the DOAS technique (Perner and Platt, 1979; Platt, 1994; Platt and Stutz, 2008) and the WinDOAS software package (Fayt and Van Roozendael, 2001). For further details, see Volkamer et al. (2015). The accuracy of our O₄ measurements has been assessed in a pure Rayleigh atmosphere (Spinei et al., 2015) and in the presence of aerosol (Volkamer et al., 2015). We found no need to apply a correction factor to the measured O₄ (Wagner et al., 2009; Spinei et al., 2015; Volkamer et al., 2015).

BrO, IO and NO₂ dSCD data used for both the OE and the parameterization retrievals are quality filtered for instrument and data analysis effects as well as cloud filtered. The color ratio of the measured intensities at 477 and 640 nm is used to identify clouds in the telescope’s field of view and in close proximity. Once the color ratio falls below 2.1 for aircraft altitudes above 4 km and below 1.95 for aircraft altitudes below 4 km, dSCD data are filtered. The altitude distinction accounts for the color ratio also being affected by aerosol extinction, which is typically higher closer to the surface. Color ratio thresholds are determined empirically and work well for most TORERO flights. To ensure that only cloudy dSCD data get filtered, the color ratio filter is manually checked for each flight and changed if needed, based on flight video data. The profile case studies discussed in Sect. 5.3 are predominantly cloud free.
5.2 Optimal estimation profiles and parameterization retrieval

5.2.1 Optimal estimation

Concentration profiles for BrO, IO and NO$_2$ were retrieved from TORERO data by linear inversion of measured dSCDs using OE. The RTM McArtim was used to calculate weighting functions that serve as OE input. Radiation fields were constrained by in situ pressure, temperature and water vapor measurements. CU AMAX-DOAS observations of O$_3$ at 360 and 477 nm were used to determine local aerosol extinction in a first step. Retrieved extinction profiles were then included in the RTM to calculate weighting functions for the inversion. The number of independent concentration points is typically well aligned with the vertical resolution of the inversion. Control over radiative transfer has been demonstrated by comparison with in situ and modeled H$_2$O data, with modeled NO$_2$, and comparison with aerosol extinction retrieved from high spectral resolution lidar (HSRL) and from Mie calculations based on aerosol size distributions measured by an in situ ultra-high-sensitivity aerosol spectrometer (UHSAS) (Volkamer et al., 2015).

5.2.2 Parameterization

The parameterized retrieval uses an almost identical RTM atmosphere, but pressure, temperature and water vapor data are averaged over each full flight, which saves RTM computation time. This averaging is possible for the TORERO study area, because air masses for each flight are rather homogenous. Reference spectra for both parameterization and OE dSCDs are identical, with one fixed reference per flight. Using a fixed reference is for practical reasons. The number of reference spectra suitable for the parameterization method is limited in the TORERO data set, particularly because zenith references for BrO and NO$_2$ need to be close in time to the O$_3$ EA 10$^\circ$ references. Not all flights provide more than one set of suitable reference spectra. To keep results comparable between flights, each flight is analyzed with one fixed reference. Further selection guidelines for references are discussed in Volkamer et al. (2015). Since atmospheric conditions found in the TORERO study area are well represented in the sensitivity studies above, the same Box-AMFs and polynomial coefficients for the interpolation of measured O$_3$ dSCDs are used. Every research flight but one, RF08, provided atmospheric conditions, where O$_3$ dSCD measurements from aircraft altitudes above 12 km could be considered Rayleigh measurements. Typically an upward angle scan covering EA 0, 1, 2, 5 and 10$^\circ$ was used to absolutely scale measured O$_3$ dSCDs (see also Spinei et al., 2015). Atmospheric conditions that pass the above introduced cloud filter are instances where the aircraft flies high above low cloud layers or vice versa. A series of preliminary sensitivity studies with cloud layers at different altitudes and trace gas profiles similar to the c profiles here (Fig. 3) has shown that the ratio of measured and modeled O$_3$ dSCDs can serve as indicator for specific cloud situations. When flying above low cloud layers, VMR$_{\text{para}}$ are typically retrieved within the established error bounds as long as the O$_4$ dSCD ratio stays below 1.15 at 360 nm and below 1.2 at 477 nm. For ratios between 1.15 and 1.3 at 360 nm and 1.2 and 1.4 at 477 nm, the measured O$_4$ dSCD is scaled to the equivalent of a 1.15 and 1.2 ratio respectively. Here, five percentage points are added to the error bound. Data points with higher O$_4$ ratios are filtered. When flying below a cloud cover, most data are retrieved within error bounds as long as the O$_4$ ratio is larger 0.5. Once it falls below 0.5 and the color ratio is larger 2.8, data are filtered out. All data points within 2 km of a solid cloud layer are filtered. HSRL data are used to get information on cloud layer heights. Overall, the cloud information gained from the O$_4$ ratios is very consistent with HSRL observations. Figure S12 provides examples of O$_4$ ratios and HSRL data for different aerosol and cloud scenarios. Note that our cloud handling here is optimized for atmospheric conditions in the TORERO study area. Further sensitivity studies are warranted in other atmospheric settings, e.g., in instances where high aerosol extinction is present at higher altitudes.

Trace gas profile information above aircraft maximum altitude for BrO and NO$_2$ is taken from RAQMS. Corrections for dSCD contributions from outside S are based on Eqs. (6)–(9) for NO$_2$ and IO. In order to calculate AMF$_{\text{ref}}$ used in Eqs. (8) and (9), AMF$_{\text{ref}}$ is scaled with the stratospheric geometric AMF, i.e., AMF = 1/cos(SZA), which saves RTM computation time. Stratospheric BrO VCDs are quantified by RAQMS, since the TORERO data set does not contain a sufficient amount of high signal-to-noise EA 10$^\circ$ spectra. Maximum BrO dSCD$_{\text{strat}}$ (Eq. 8) values are typically around 1–2 $\times$ 10$^{13}$ molec cm$^{-2}$ at SZA = 60$^\circ$, which is on the order of the EA 0° dSCD fit error. Select comparison of stratospheric corrections retrieved from EA 10° measurements confirm the model-based correction within an 2–3 $\times$ 10$^{13}$ molec cm$^{-2}$ uncertainty created by the EA 10$^\circ$ dSCD fit error. For NO$_2$, a typical TORERO dSCD$_{\text{strat}}$ value at 60$^\circ$ SZA is 1.5–3 $\times$ 10$^{15}$ molec cm$^{-2}$, which is about a factor of 2–4 higher than a tropospheric EA 0° dSCDs measured in pristine background air (e.g., NO$_2$ c profile). Here, our EA 10$^\circ$ dSCD fit error of 3–5 $\times$ 10$^{14}$ molec cm$^{-2}$ is almost on the same order as the tropospheric EA 0° dSCDs, underlining the need for a highly accurate characterization of the stratospheric VCD by EA 10$^\circ$ measurements. Since TORERO specifically targeted very pristine air masses, we refrained from running the NO$_2$ parameterization retrieval on the complete data set and focused instead on select case studies with dSCD$_{\text{strat}}$ $\ll$ EA 0° dSCDs. For these cases evaluation of NO$_2$ is still possible down to as low as 10 pptv, as has been demonstrated in Fig. 10 in Volkamer et al. (2015).

Layer $n_{\text{max}}$, which is the altitude that separates stratospheric and tropospheric corrections (see Sect. 2.2), is set to
Figure 7. Comparison of VMR data retrieved from TORERO AMAX-DOAS data using the parameterization retrieval (para) or optimal estimation (OE) for select BrO (left), IO (middle) and NO$_2$ (right) profiles.

the maximum aircraft altitude for which the $i = 0$ parameterization retrieval provides profile information. The layer $n_{max}$ is identical to the maximum aircraft altitude of each individual flight, unless high-altitude dSCD data have been filtered (clouds/quality assurance). Most TORERO flights targeted air masses that are rather homogenous with respect to trace gas distributions. In order to calculate dSCD$_{\text{top}}^i$ and $f_{\text{IO}}^i$ (Eqs. 2 and 7), retrieved concentrations are averaged over the full flight, then interpolated and smoothed where needed, to minimize data scatter effects on the trace gas profile shape correction. During instances where the flight track crossed into stratospheric air, a second profile for BrO and NO$_2$ is created and used to calculate dSCD$_{\text{top}}^i$ and $f_{\text{IO}}^i$ for these time periods. IO VMR data often showed stronger variations below 5 km altitude within one flight. Here, up to three separate profiles per flight were created, while ensuring that profile-dependent differences above 5 km in the final VMR$_{\text{para}}$ do not exceed error bounds. For the direct profile comparison discussed in the following section, the calculation of dSCD$_{\text{top}}^i$ and $f_{\text{IO}}^i$ is based on results from the profile time period only. The errors reported for the parameterized data are those discussed above and in Sect. 4.3. In order to avoid a potential high bias created by filtering quality-assured dSCD data below the dSCD limit (see Sect. 3.2), respective VMR$_{\text{para}}$ points are set to 0.2, 0.02 and 4 pptv for BrO, IO and NO$_2$ respectively.

5.3 Comparison of optimal estimation and parameterization profiles

Figure 7 shows a comparison of VMR data retrieved by OE and by the parameterization method for select profiles of BrO, IO and NO$_2$ from the TORERO campaign for flights RF01, RF12 and RF17 (Volkamer et al., 2015; Wang et al., 2015). Parameterized VMRs are reported at aircraft altitude, i.e., the altitude for which the Box-AMFs are calculated. The spread seen within the same grid layer could be a reflection of a true trace gas gradient. Here the parameterization retrieval can provide additional information that is lost to the smoothing error of the OE method. The pronounced IO layer in the RF01 profile presents a good example of this effect. The VMR$_{\text{para}}$ data points between 1.9 and 2.4 km clearly outline the IO peak at 2.25 km, whereas the OE data report discrete values for 1.75, 2.25 and 2.75 km. Note that the lines connecting the OE data points in Fig. 7 are only plotted to help guide the eye along the profile shape. All data points overlap within error bars, but the parameterization reveals steeper IO gradients indicative of less smoothing. In order to calculate correlations, the VMR$_{\text{OE}}$ data are interpolated to the VMR$_{\text{para}}$ data. Results for all three trace gases are shown in Fig. 8. To increase statistics for the correlation, trace gas profiles from more flights are included, i.e., from RF01, RF04, RF05, RF12, RF14 and RF17 for all three trace gases (see also Wang et al., 2015, and Volkamer et al., 2015). Profile selection is based on availability of high-quality OE profiles. A least orthogonal distance fit is applied to consider the $x$ and $y$ errors. Offset and slopes are reported for a 95% confidence interval and included in the individual trace gas panels. Also here the agreement between VMR$_{\text{para}}$ and VMR$_{\text{OE}}$ is excellent. Offset values are insignificant, while slopes of 0.95 ± 0.14 for BrO, 1.00 ± 0.12 for IO and 0.87 ± 0.15 for NO$_2$ are within expectations based on the sensitivity studies (see Sect. 4.3).

5.4 TORERO BrO and IO VMR$_{\text{para}}$ results

Figure 9 shows BrO and IO VMR$_{\text{para}}$ results along flight tracks for all 17 TORERO RFs (but RF08). Altitudes of retrieved VMR data are plotted over latitude and are color coded by mixing ratios. BrO is consistently low in the boundary layer and almost never exceeds the detection limit of 0.5 pptv. Particularly in the tropical free troposphere, Fig. 9 shows a significant variability for BrO. VMRs larger 1 pptv at altitudes above 8 km are also found in air without sig-
Figure 8. Correlations of TORERO AMAX-DOAS VMR data retrieved by parameterization (para) and optimal estimation (OE) for BrO (left), IO (middle) and NO\textsubscript{2} (right). Grey shaded areas indicate 15 and 30 % error; green dashed lines show trace gas detection limits. Linear fits and fit parameter (s: slope; o: offset) are included in each panel.

Figure 9. TORERO AMAX-DOAS BrO (left) and IO (right) VMR\textsubscript{para} data for the complete campaign. Plotted are aircraft altitudes over latitude, color coded by VMR\textsubscript{para}. Longitudes covered are 70 to 105\textdegree W.

significant stratospheric influence and remain currently unexplained (Wang et al., 2015). In Fig. 10 TORERO BrO and IO VMR\textsubscript{para} results are plotted as altitude-resolved whiskers, showing the mean with its 95 % confidence interval (CI) as uncertainty and 5, 25, 75 and 95 percentiles. The parameterization method provides better statistics. As expected, IO shows maxima in the boundary layer, but also a prevalent distribution throughout the troposphere. Our data suggest the existence of a hemispheric gradient with higher IO in the southern hemisphere. Large 95 percentiles between 1 and 4 km altitude are mainly driven by the IO layers observed near Antofagasta (see Fig. 7). These layers will be discussed elsewhere. For BrO, Wang et al. (2015) had noted atmospheric variability as a primary driver for error bars in the average profiles in pristine air. The mean BrO was 3.0 pptv at 13.5 km and varied between 1.2 pptv (RF04) and 4.0 pptv (RF05). The overall data set also includes measurements in the outflow of terrestrial convection near the coast and has a lower mean BrO VMR\textsubscript{para} of 1.86 ± 0.16 pptv (95 % CI, \(N = 162\)) at 13.5 km and 1.38 ± 0.16 pptv (95 % CI, \(N = 78\)) at 14.5 km. The decrease in BrO above 14 km altitude is significant and broadly consistent with findings by Werner et al. (2016). Decreasing BrO with increasing altitude had previously been observed during the RF04 case study (Wang et al., 2015). Notably, VMR\textsubscript{para} and VMR\textsubscript{OE} are consistent to better 15 % for all case study profiles discussed in our earlier work (see Fig. 8); these case studies had probed primarily air masses influenced by convection over oceans. The lower mean BrO in Fig. 10 compared to Fig. 2 of Wang et al. (2015) is hence primarily reflecting different air mass histories, consistent with the variability in Br\textsubscript{y}, and the hypothesis that sea-salt-derived Br\textsubscript{y} is a source for BrO in the upper free troposphere downwind of marine convection (Wang et al., 2015).

The observed halogen vertical distribution over the tropical Eastern Pacific appears to be complex and is not yet fully understood. Notably, recent measurements of low BrO in the tropical transition layer (TTL) over the tropical Eastern Pacific ocean during the ATTREX project (Werner et al., 2016) rely on knowledge about the tropospheric BrO profile below the aircraft for a priori information (Volkamer et al., 2015; Wang et al., 2015). If the TORERO observations are representative of the troposphere during ATTREX, the lower mean tropospheric BrO of VMR\textsubscript{para} in Fig. 10 suggests that current TTL BrO estimates could be lower limits.
A BrO maximum at altitudes between 12 and 14 km, with decreasing BrO at higher and lower altitudes, is currently not captured by global models (Schmidt et al., 2016; Sherwen et al., 2016a). Furthermore, aerosol bromide is frequently detected in particles in the upper troposphere and lower stratosphere (Murphy and Thomson, 2000), but the bromine mass concentration in these particles is currently not well known. The vertical distribution of BrO in the upper troposphere and lower stratosphere is affected by uncertainties and variability of Br\textsubscript{y} sources to the free troposphere (very short lived species and sea-salt derived Br\textsubscript{y}), gas-phase Br\textsubscript{y} partitioning, heterogeneous reactions on aerosol and ice surfaces, uncertain particulate bromide mass in the free troposphere and uncertainties about Br\textsubscript{y} wet deposition. Simultaneous measurements of BrO, other gas-phase Br\textsubscript{y} species and particulate bromide are desirable.

The parameterization retrieval of VMRs along complete flight tracks enables a summary view of AMAX-DOAS results, which allows an assessment on the consistency of data variability or gradients across the whole study area. Based on the number of available EA 0° spectra, a parameterization duty cycle is defined, which expresses the fraction of EA 0° dSCD measurements that are converted into VMRs. A total of 7124 BrO dSCD measurements and 7168 IO dSCD measurements were processed. Due to data quality, cloud and parameterization method filters, respectively, 24.3, 22.4 and 10.3% of the BrO data points and 10.6, 26.2 and 3.2% of the IO data points were filtered. The resulting duty cycle for the quality-assured VMR retrievals were 55.4% for BrO and 81.4% for IO before cloud filters and 44.3 and 60.1% for BrO and IO after cloud filters. Notably, the method filter removes the least number of data points for both trace gases, which underlines the statistical advantage of the parameterization method over OE. Based on these numbers, the development of an advanced cloud treatment has good potential to further improve the duty cycle.

6 Conclusions and outlook

The parameterization retrieval is a robust tool to convert AMAX-DOAS EA 0° dSCDs of BrO, IO and NO\textsubscript{2} directly into VMRs along a flight track. Flight tracks that vary with altitude frequently provide the best results, because the iterative approach increases the accuracy of VMR\textsubscript{para} by utilizing profile information gained from ascent or descent measurements. The magnitude of the stratospheric correction is constrained from measurements of EA 10° dSCD at high altitude. Based on our sensitivity studies on simulated data and application to field data, we conclude the following:

- The method is applicable over a wide range of atmospheric conditions and measurement geometries. VMRs of trace gases with significant stratospheric contributions to the VCDs can be retrieved for SZAs 0 to 60° and for tropospheric trace gases for SZAs 0 to 70°, the latter being the full range covered by our sensitivity studies. VMR\textsubscript{para} data are on average within 10–15% of VMR\textsubscript{true}. Errors that arise from suboptimal reference spectra are either accounted for by the dSCD\textsubscript{c} correction or are avoided by applying filters. Actively minimizing SCD\textsubscript{ref} based on reference selection improves the accuracy of the parameterization retrieval.

- The comparison of VMR\textsubscript{para} field data with VMR\textsubscript{OE} shows excellent agreement within the error bounds established by the sensitivity studies. Correlations of 13% and better are within expectations and further corroborate that the parameterization retrieval is suitable for the analysis of field data.

- Using O\textsubscript{4} dSCDs as scaling factors for aerosol extinction is a viable tool for altitude ranges between 0 and 15 km but not at higher altitudes, where O\textsubscript{4} contributions from outside S are a significant fraction of the measured O\textsubscript{4} dSCDs and become difficult to account for.

- The retrieval is straightforward for gases that do not have a significant presence in the stratosphere. For gases with a significant presence in the stratosphere, the error can be reduced by following the recommendations given in Sect. 4.3.3.

- The TORERO VMR retrieval has a duty cycle of 55.4 and 81.4% for BrO and IO before cloud filtering and 44.3 and 60.1% after. Less than 11% of data points are removed by the method filters, which underlines the statistical advantage of the parameterization method over OE.
TORERO BrO and IO retrievals show halogen abundances over the tropical Eastern Pacific that are not completely understood, with implications for ozone depletion, atmospheric oxidation capacity and mercury oxidation (Wang et al., 2015; Schmidt et al., 2016; Sherwen et al., 2016a, b). Significant features like the BrO decrease above 14 km or the elevated IO layers near Antofagasta warrant further investigation. For future use, the method can easily be adapted for the retrieval of other absorbers like glyoxal, formaldehyde or HONO. The inherently fast conversion of dSCDs into VMRs can also serve as a tool for near-real-time VMR retrievals in the field. Future work will include optimizing the parameterization retrieval for (1) polluted environments, i.e., atmospheres with high NO$_2$ and/or aerosol extinction; (2) SZA conditions outside current filters’ and (3) minimizing the need for cloud filtering.

7 Data availability

The AMAX-DOAS BrO and IO data are available from the TORERO data archive: http://data.eol.ucar.edu/master_list/?project=TORERO. The TORERO data set is open for use by the public, subject to the following data policy: https://www.eol.ucar.edu/node/4527. The archive contains aircraft and atmosphere state parameters, in situ measurements, flight videos and RAQMS and HSRL data. Specialized AMAX-DOAS data products can be obtained from the authors upon request.

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